



# Land Retrieval from PolSAR

**Eric POTTIER**  
**20 / 11 / 2019**

ESA–MOST China Dragon 4 Cooperation

2019 ADVANCED INTERNATIONAL TRAINING COURSE IN LAND REMOTE SENSING

中欧科技合作“龙计划”第四期 2019年陆地遥感高级培训班

18 to 23 November 2019 | Chongqing University, P.R. China



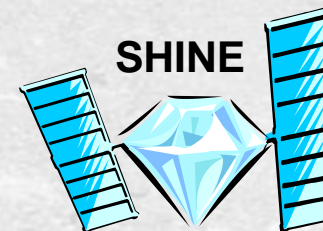
培训时间: 2019年11月18日-23日 主办方: 重庆大学



**Eric POTTIER**  
[eric.pottier@univ-rennes1.fr](mailto:eric.pottier@univ-rennes1.fr)

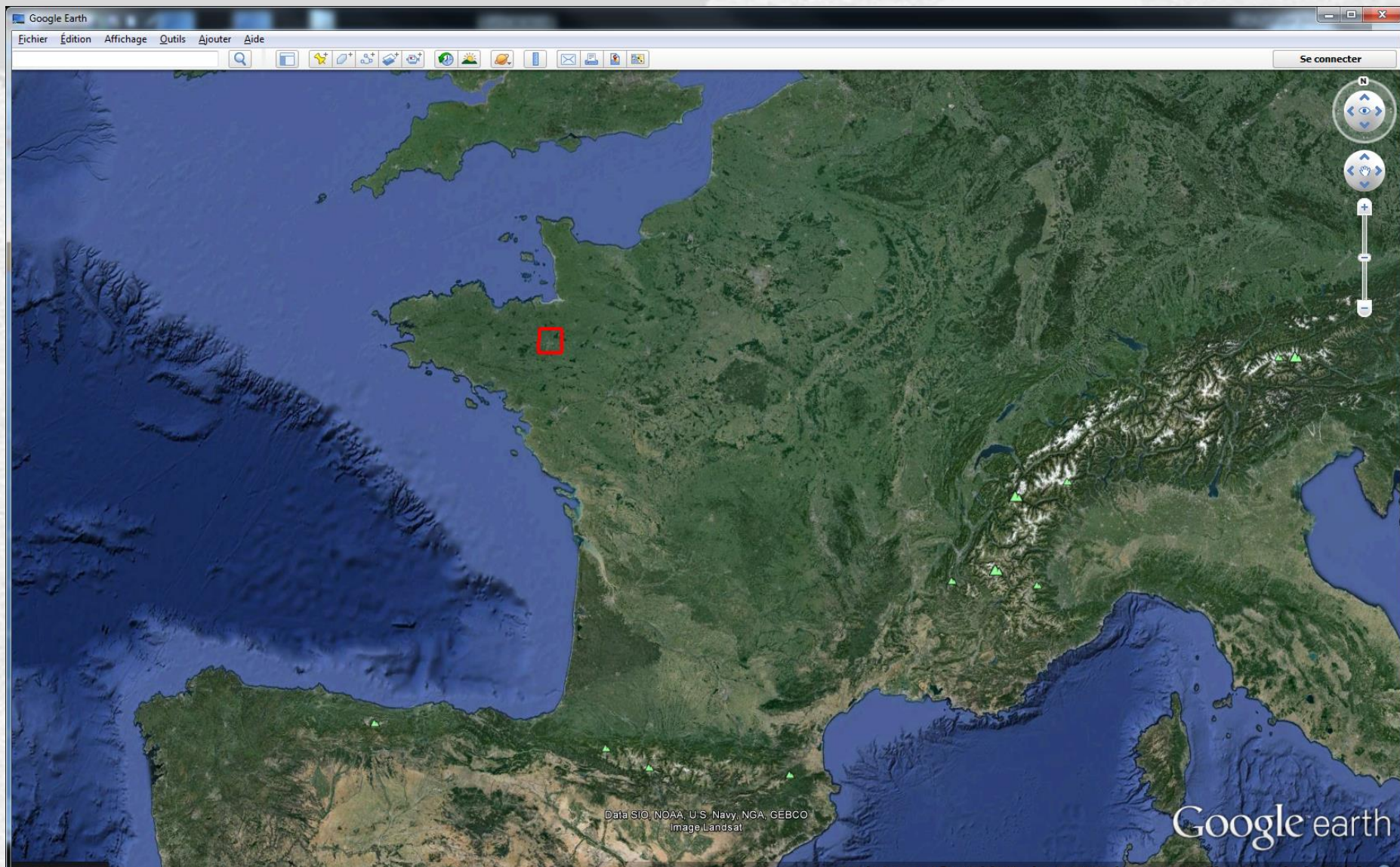


**I.E.T.R. - UMR CNRS 6164**  
Université de Rennes I - Campus de Beaulieu  
Pôle Micro Ondes Radar - Bat 11D  
263 Avenue Général Leclerc  
CS 74205 - 35042 Rennes Cedex – France

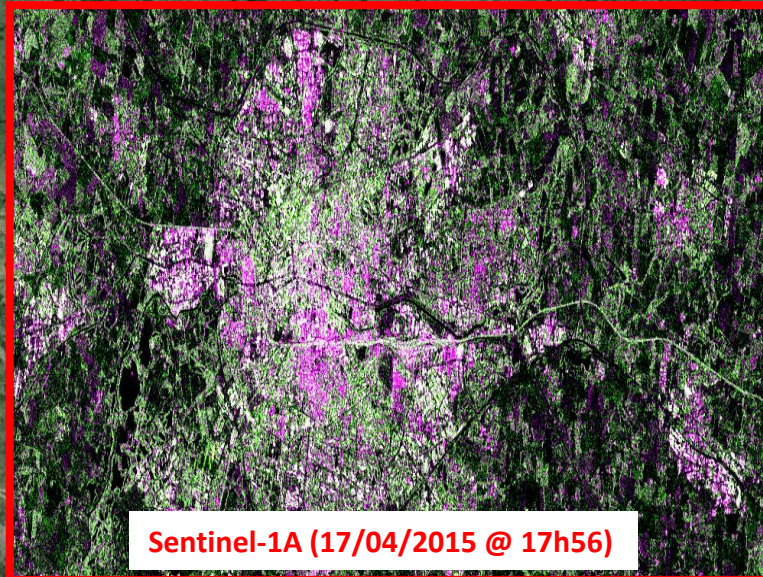
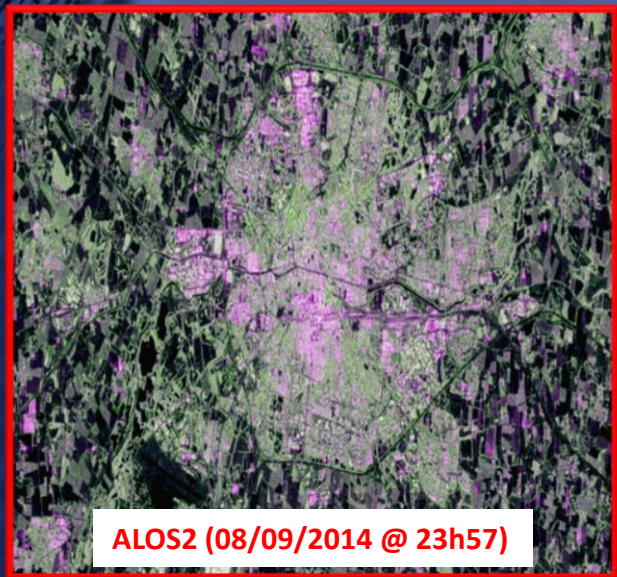
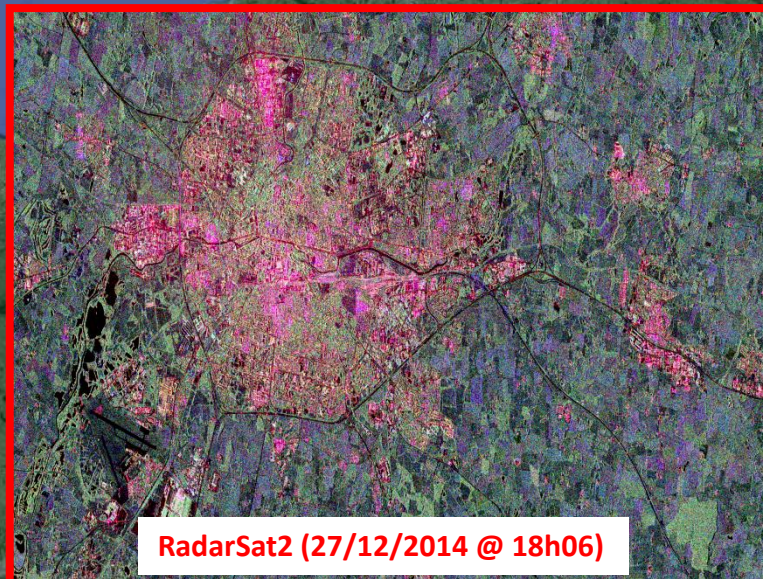


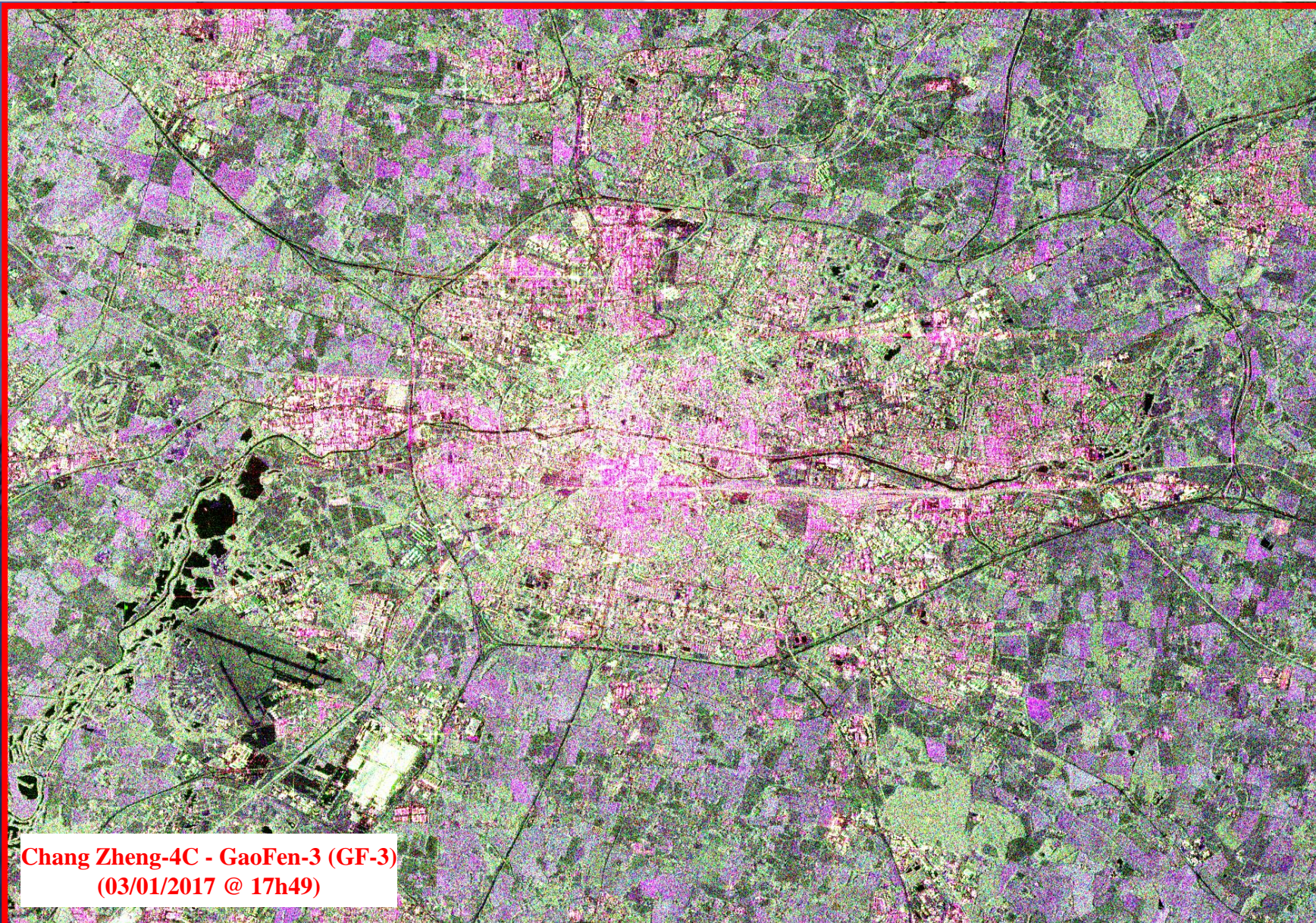
**SAR & Hyperspectral multi-modal Imaging**  
**and signal processing,**  
**Electromagnetic modeling**





# RENNES - BRITANNY - FRANCE

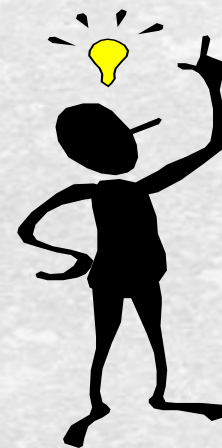




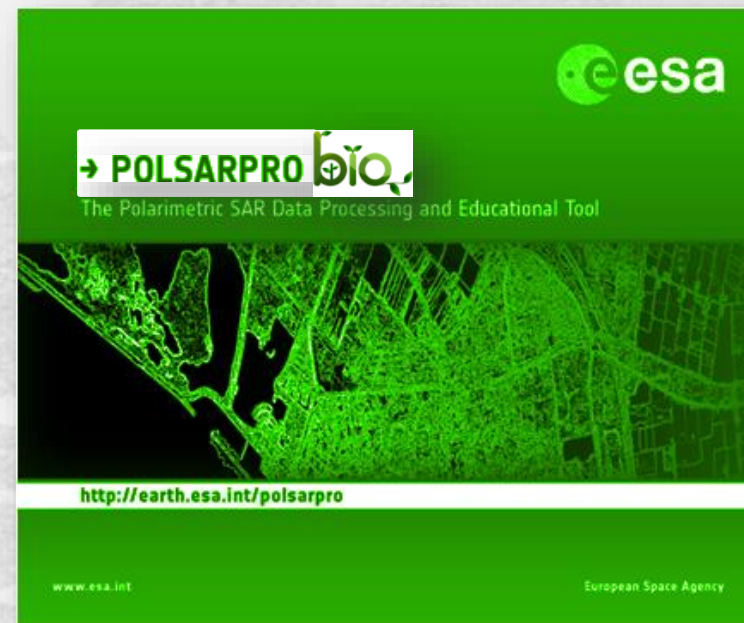
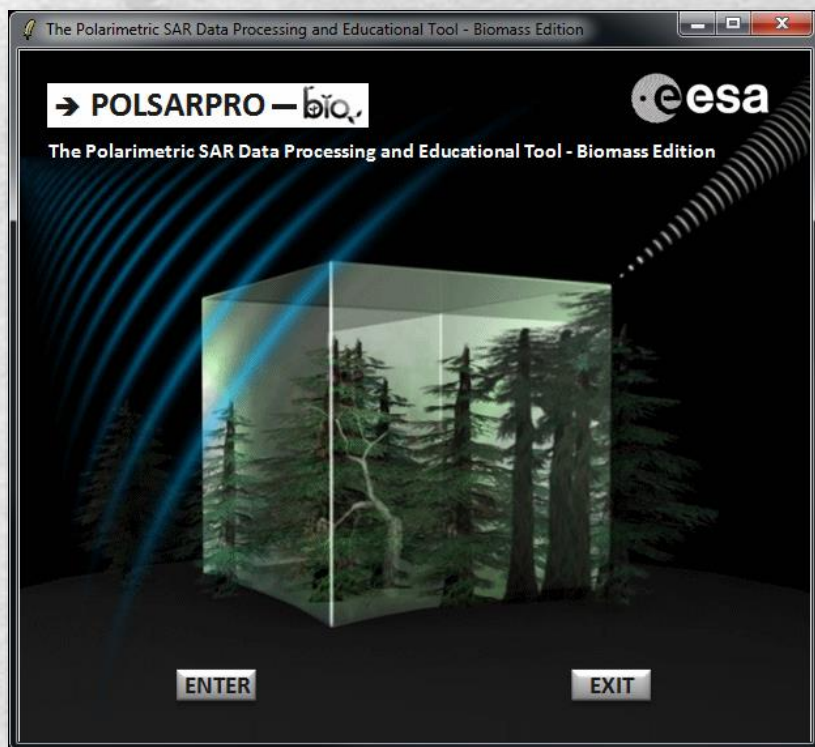
**Chang Zheng-4C - GaoFen-3 (GF-3)**  
**(03/01/2017 @ 17h49)**

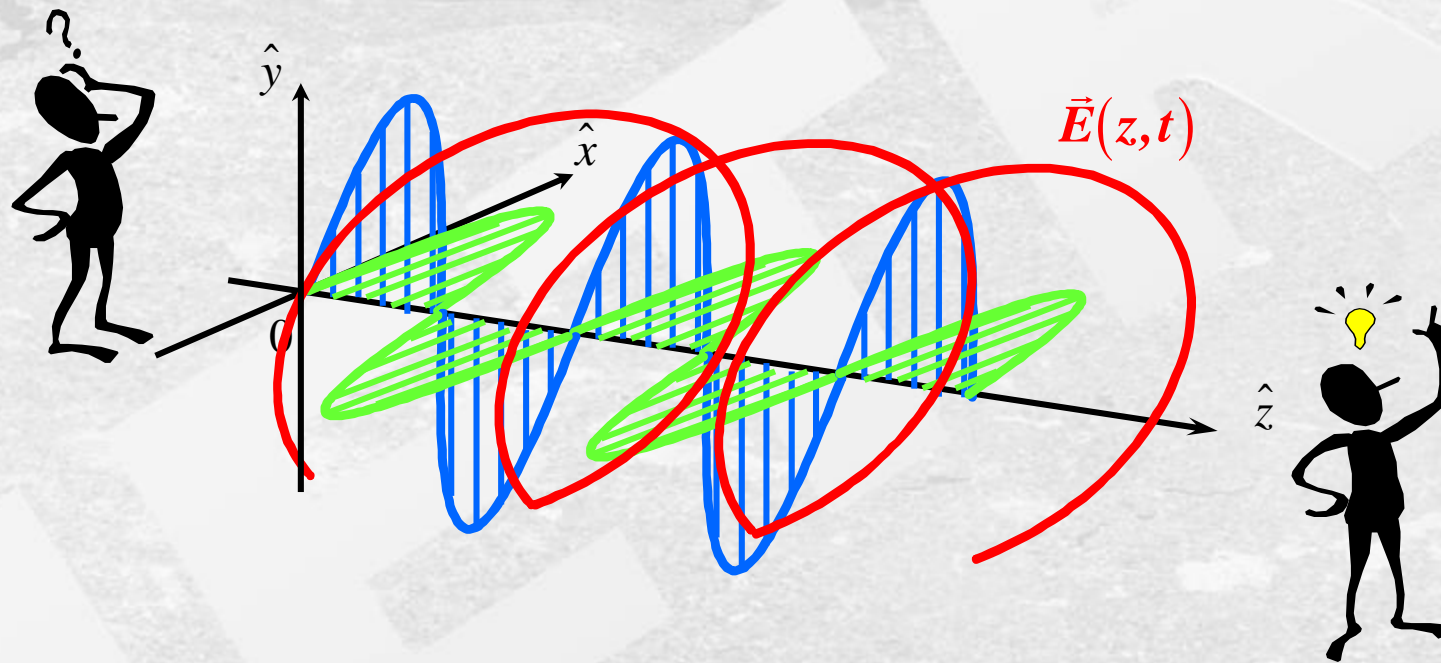


**Objective**  
**To provide**  
**the minimum, but necessary,**  
**amount of knowledge required**  
**to understand**  
**scientific works on**  
**Radar Polarimetry**



## Practicals





# DATASETS

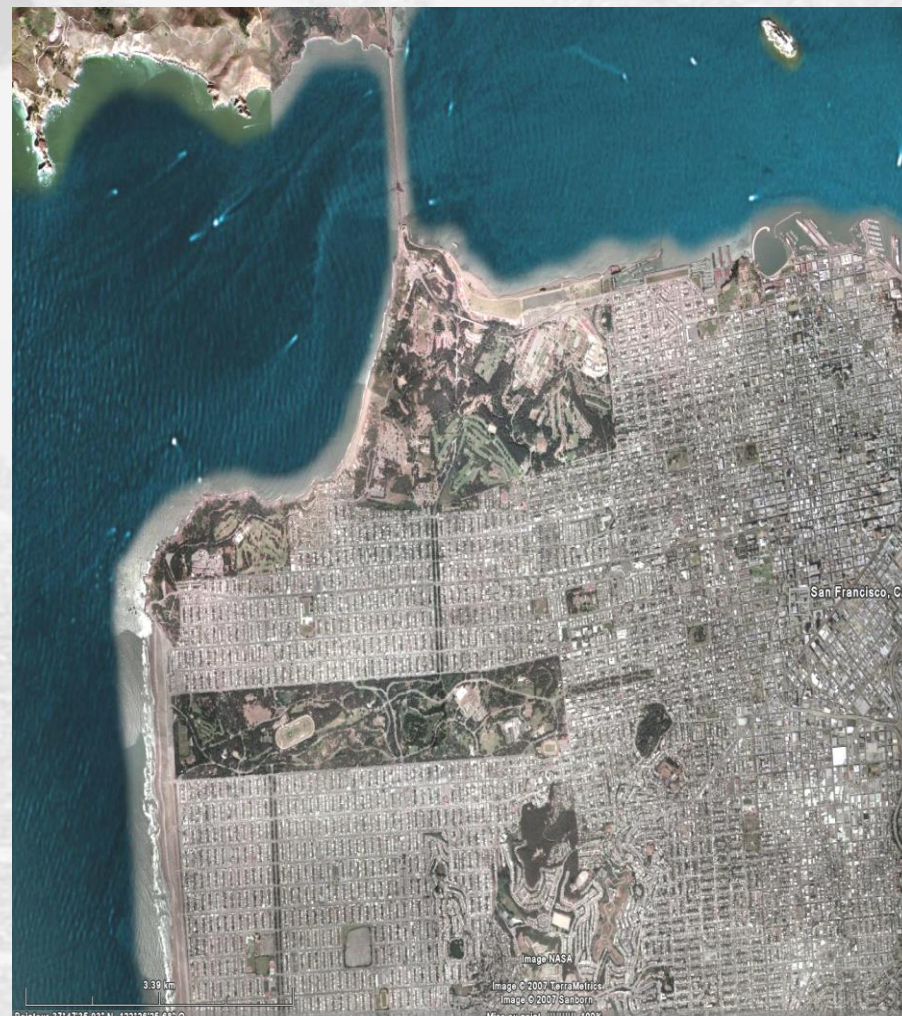




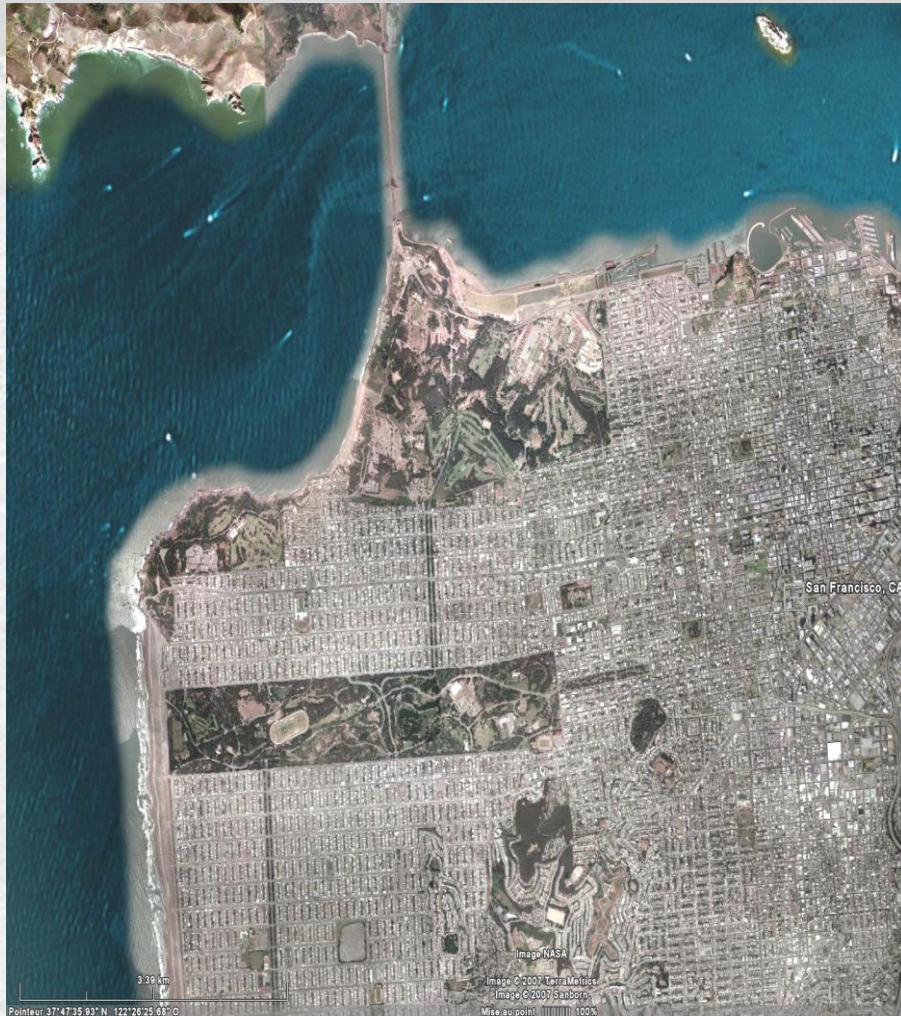
**AIRSAR JPL**

**DC8**

**P, L, C-Band (Quad)**



© Google Earth



© Google Earth



**|HH+VV|**  
 **$T_{11}=2A_0$**

**|HV|**  
 **$T_{33}=B_0-B$**

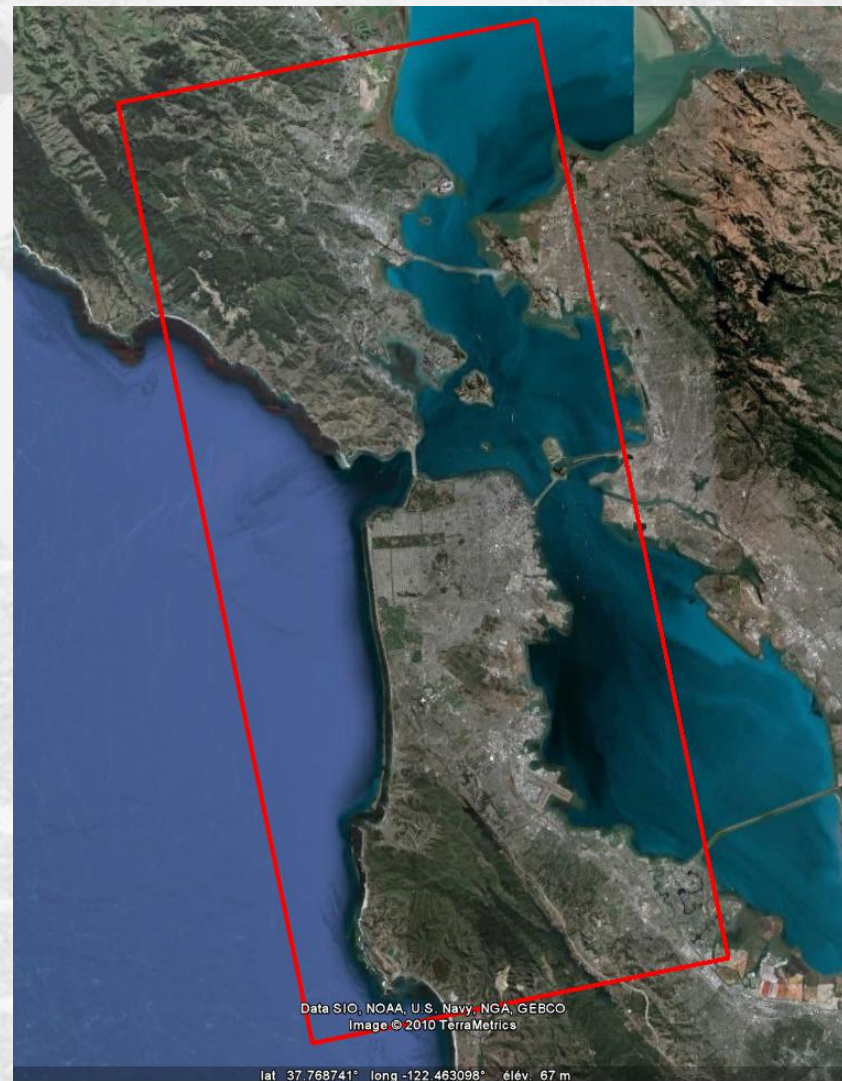
**|HH-VV|**  
 **$T_{22}=B_0+B$**



## ALOS - PALSAR

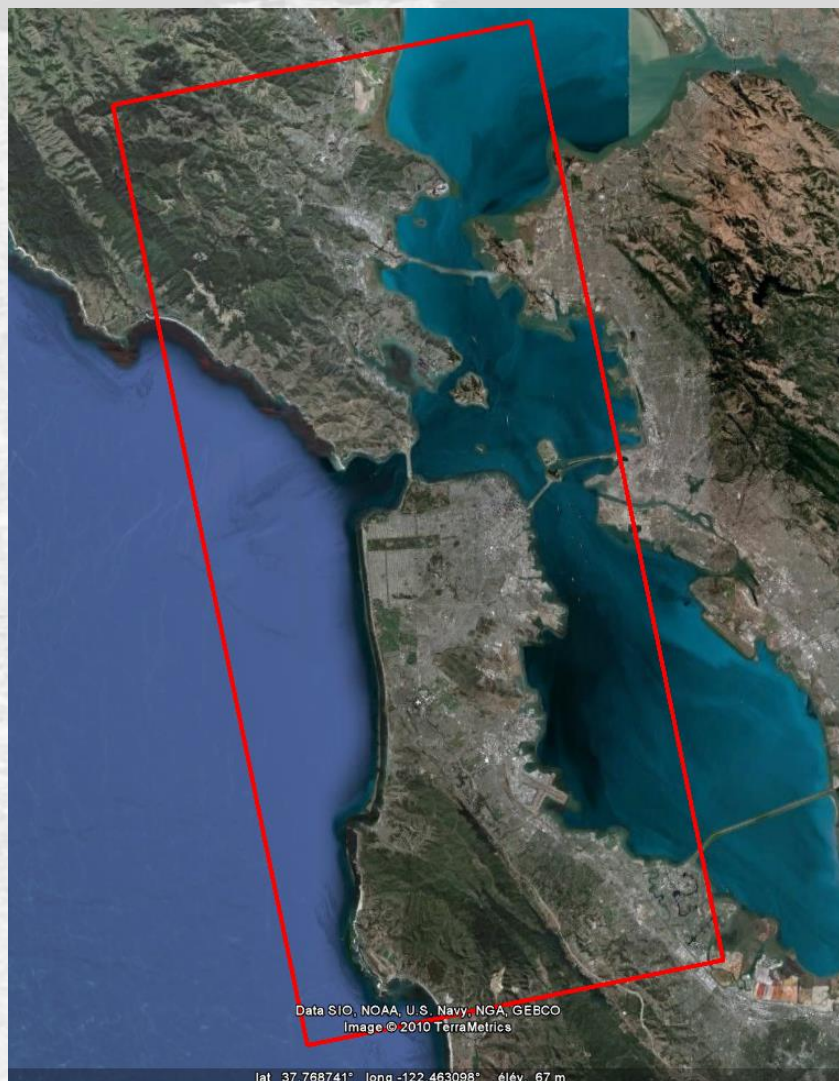


### L-Band (Quad)

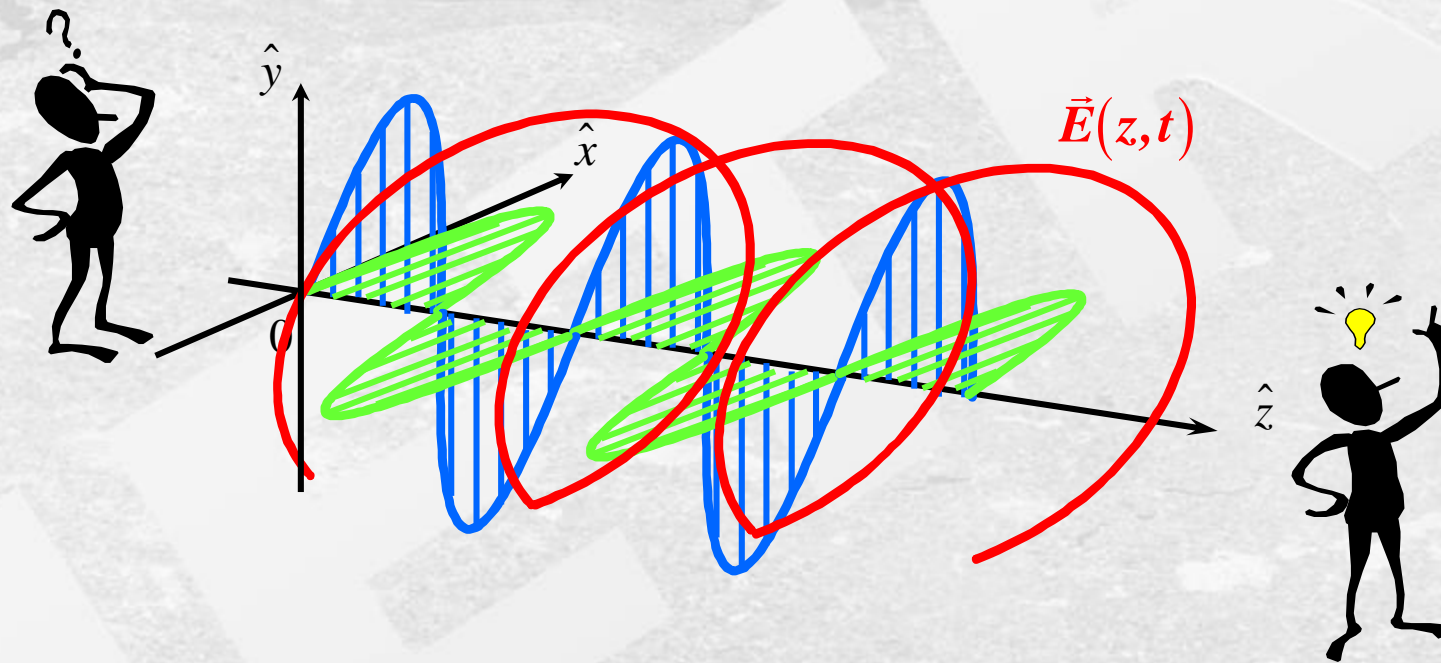


© Google Earth

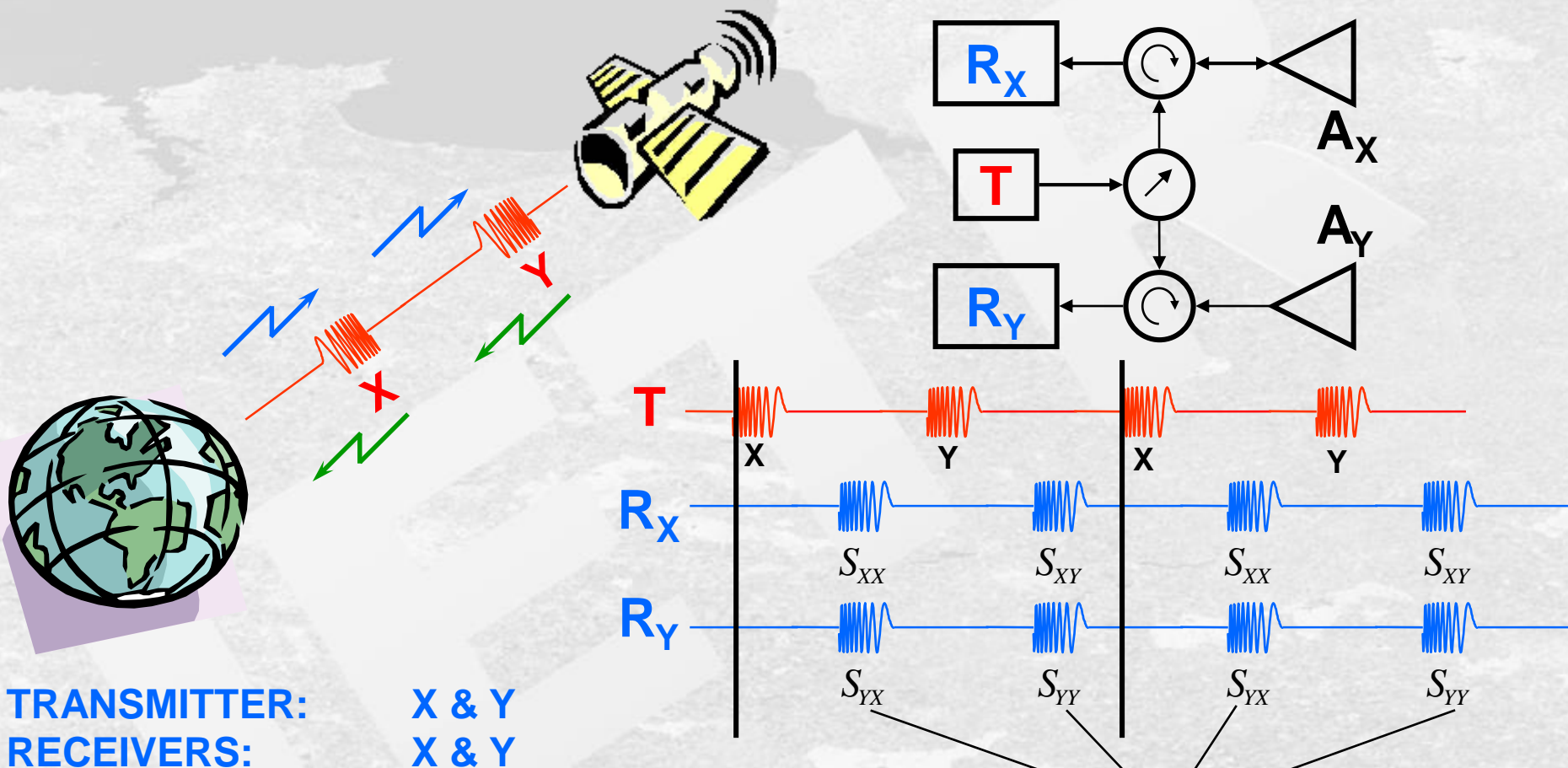




Courtesy of Dr Don Artwood (ASF)



# SUMMARY



**SINCLAIR MATRICES**

$$[S] = \begin{bmatrix} S_{XX} & S_{XY} \\ S_{YX} & S_{YY} \end{bmatrix}$$

**SCATTERING POLARIMETRY**

Tx → Rx →

Tx → Rx ↑

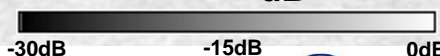
Tx ↑ Rx ↑



$|HH|_{dB}$

$|HV|_{dB}$

$|VV|_{dB}$



## Sinclair Color Coding



© Google Earth

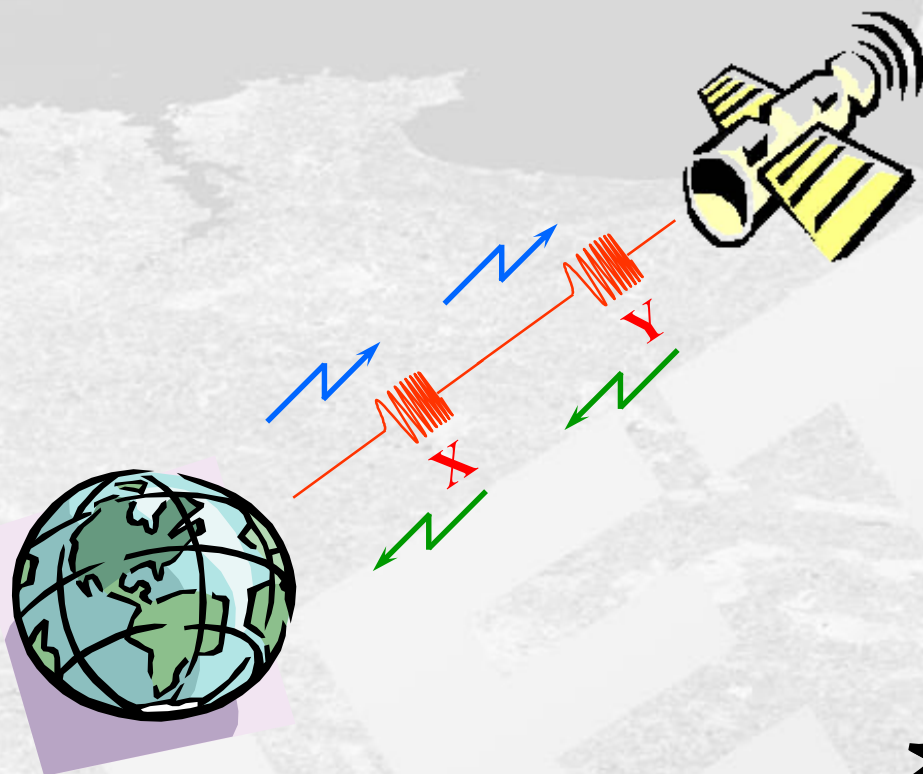


|HH|

|HV|

|VV|



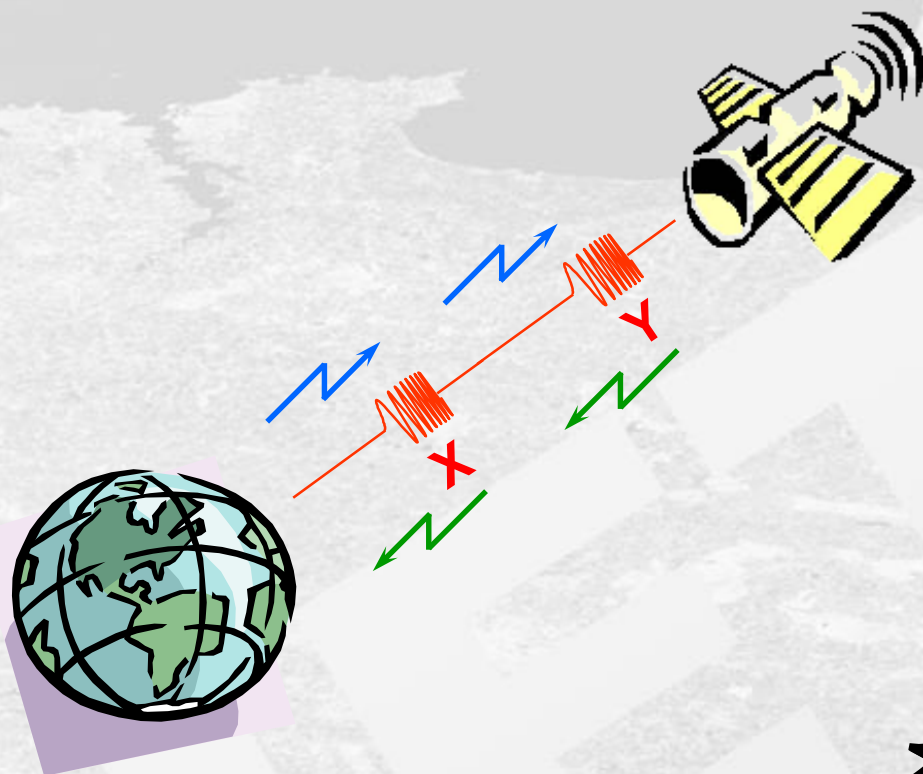


TRANSMITTER:  
RECEIVERS:

X & Y  
X & Y

## THE DIFFERENT TARGET POLARIMETRIC DESCRIPTORS

- [S] SINCLAIR Matrix
- $\underline{k}, \underline{\Omega}$  Target Vectors
- [K] KENNAUGH Matrix
- [T] Coherency Matrix
- [C] Covariance Matrix



TRANSMITTER: X & Y  
RECEIVERS: X & Y

## THE DIFFERENT TARGET POLARIMETRIC DESCRIPTORS

- [S] SINCLAIR Matrix
- [K] KENNAUGH Matrix
- $\underline{k}, \underline{\Omega}$  Target Vectors
- [T] Coherency Matrix**
- [C] Covariance Matrix

STATISTICAL DESCRIPTION  
PARTIAL SCATTERING POLARIMETRY

## MONOSTATIC CASE

### PAULI SCATTERING VECTOR $\underline{k}$

$$\underline{k} = \frac{1}{\sqrt{2}} \begin{bmatrix} S_{XX} + S_{YY} & S_{XX} - S_{YY} & 2S_{XY} \end{bmatrix}^T$$



### COHERENCY MATRIX $[T]$

$$[T] = \underline{k} \cdot \underline{k}^{*T} = \begin{bmatrix} 2A_0 & C - jD & H + jG \\ C + jD & B_0 + B & E + jF \\ H - jG & E - jF & B_0 - B \end{bmatrix}$$

HERMITIAN POSITIVE SEMI-DEFINITE MATRIX - RANK 1

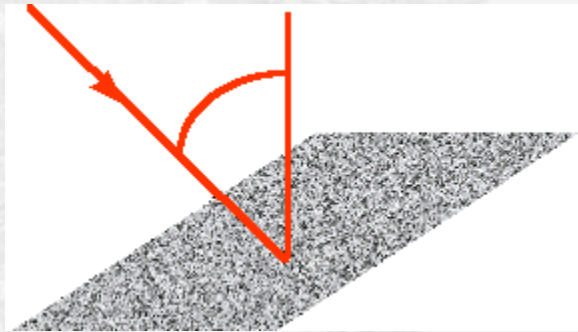
### HUYNEN TARGET GENERATORS

$$T_{11} = 2A_0 = |S_{XX} + S_{YY}|^2 \quad T_{22} = B_0 + B = |S_{XX} - S_{YY}|^2$$

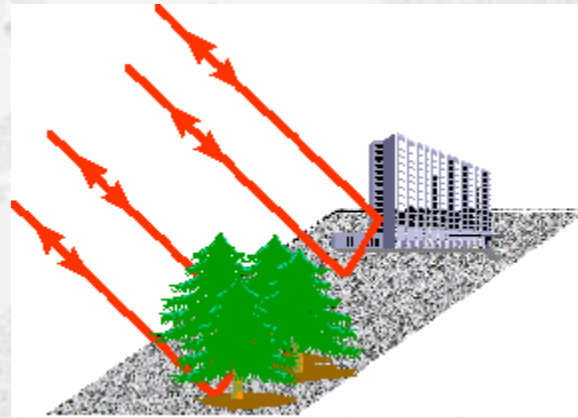
$$T_{33} = B_0 - B = 2|S_{XY}|^2$$

## PHYSICAL INTERPRETATION

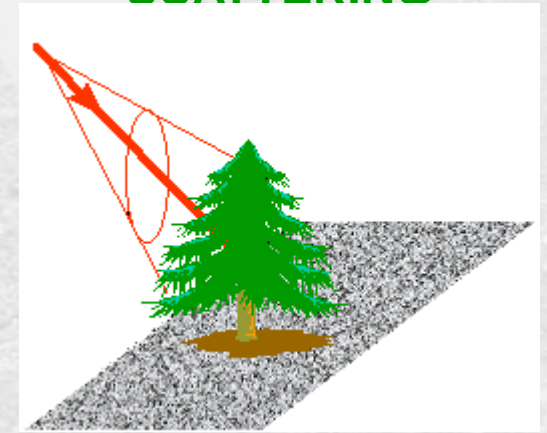
### SINGLE BOUNCE SCATTERING (ROUGH SURFACE)



### DOUBLE BOUNCE SCATTERING



### VOLUME SCATTERING



$$T_{11} = 2A_0 = |S_{XX} + S_{YY}|^2$$

$$T_{33} = B_0 - B = 2|S_{XY}|^2$$

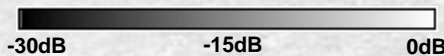
$$T_{22} = B_0 + B = |S_{XX} - S_{YY}|^2$$



$|HH+VV|_{dB}$



$|HV|_{dB}$



$|HH-VV|_{dB}$

## (H,V) POLARISATION BASIS



© Google Earth



**|HH+VV|**

**|HV|**

**|HH-VV|**

### SINCLAIR MATRIX

$$[S] = \begin{bmatrix} S_{XX} & S_{XY} \\ S_{YX} & S_{YY} \end{bmatrix}$$



### SCATTERING VECTOR $\underline{k}$

$$\underline{k} = \frac{1}{\sqrt{2}} \begin{bmatrix} S_{XX} + S_{YY} & S_{XX} - S_{YY} & 2S_{XY} \end{bmatrix}^T$$

### COHERENCY MATRIX $[T]$

$$[T] = \underline{k} \cdot \underline{k}^{*T}$$

## SINCLAIR MATRIX

$$[S_{(B, B_{\perp})}] = [U_{(A, A_{\perp}) \rightarrow (B, B_{\perp})}]^T [S_{(A, A_{\perp})}] [U_{(A, A_{\perp}) \rightarrow (B, B_{\perp})}]$$

## CON-SIMILARITY TRANSFORMATION

$$[U_{3(A, A_{\perp}) \rightarrow (B, B_{\perp})}]$$

U(3) SPECIAL UNITARY ELLIPTICAL BASIS TRANSFORMATION MATRIX



## COHERENCY MATRIX

$$[T_{(B, B_{\perp})}] = [U_{3(A, A_{\perp}) \rightarrow (B, B_{\perp})}] [T_{(A, A_{\perp})}] [U_{3(A, A_{\perp}) \rightarrow (B, B_{\perp})}]^{-1}$$

## SIMILARITY TRANSFORMATION



## SPECIAL UNITARY SU(2) GROUP

$$[U_2] = [U_2(\phi)] [U_2(\tau)] [U_2(\alpha)]$$

$$= \begin{bmatrix} \cos(\phi) & -\sin(\phi) \\ \sin(\phi) & \cos(\phi) \end{bmatrix} \begin{bmatrix} \cos(\tau) & j \sin(\tau) \\ j \sin(\tau) & \cos(\tau) \end{bmatrix} \begin{bmatrix} e^{-j\alpha} & 0 \\ 0 & e^{j\alpha} \end{bmatrix}$$

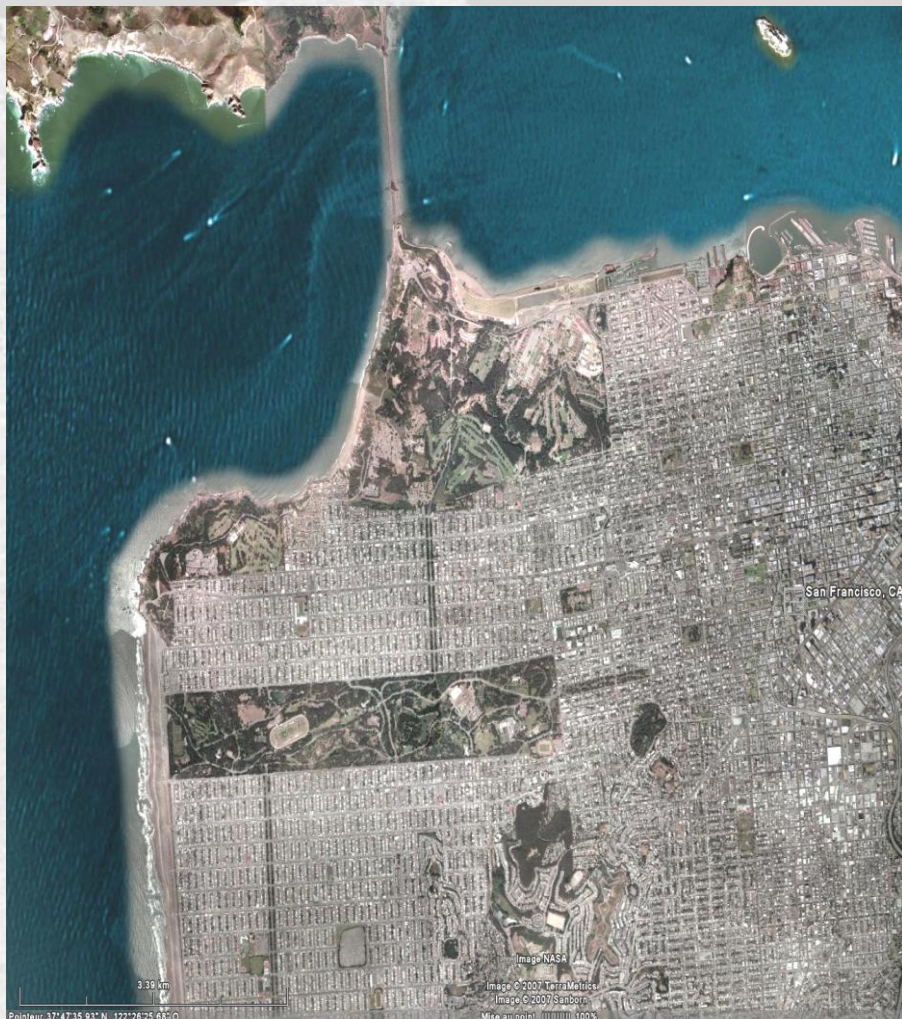


## SPECIAL UNITARY SU(3) GROUP

$$[U_3(2\phi)] [U_3(2\tau)] [U_3(2\alpha)]$$

$$= \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos(2\phi) & \sin(2\phi) \\ 0 & -\sin(2\phi) & \cos(2\phi) \end{bmatrix} \begin{bmatrix} \cos(2\tau) & 0 & j \sin(2\tau) \\ 0 & 1 & 0 \\ j \sin(2\tau) & 0 & \cos(2\tau) \end{bmatrix} \begin{bmatrix} \cos(2\alpha) & -j \sin(2\alpha) & 0 \\ -j \sin(2\alpha) & \cos(2\alpha) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

## (H,V) POLARISATION BASIS



© Google Earth



|HH+VV|

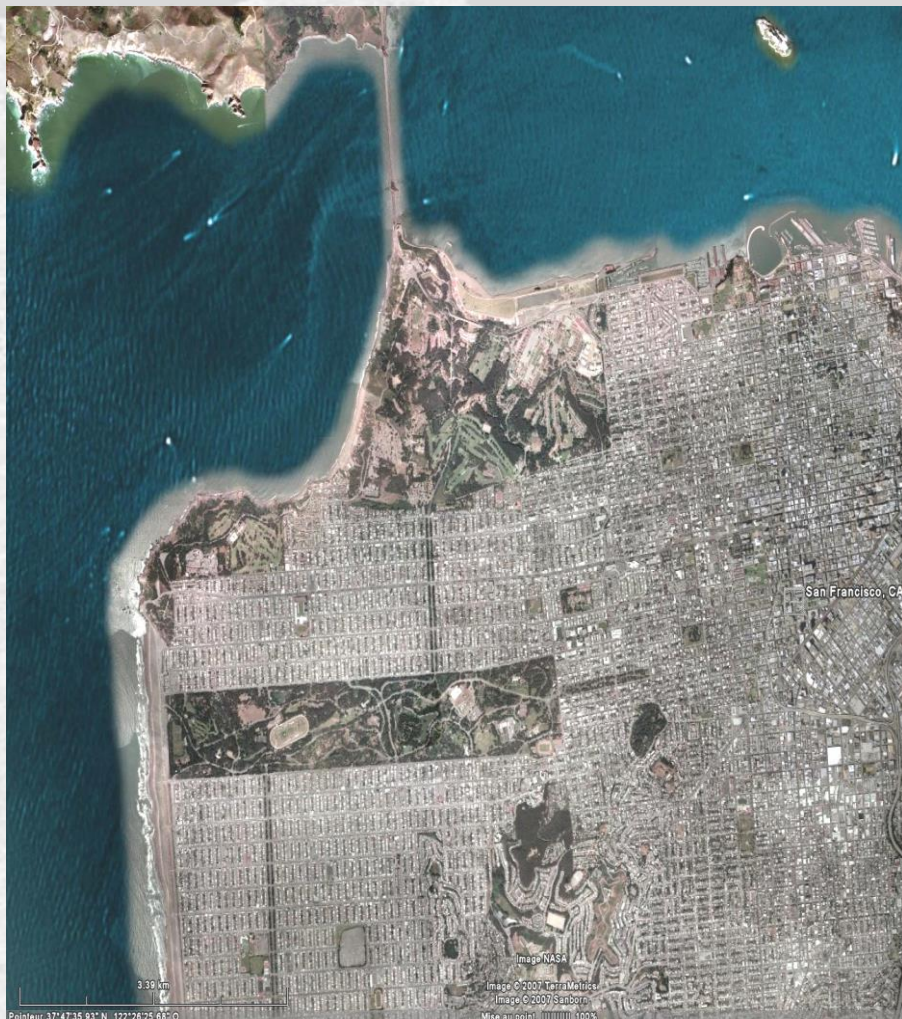
|HV|

|HH-VV|

# ELLIPTICAL BASIS TRANSFORMATION



(+45°,-45°) POLARISATION BASIS



© Google Earth



|AA+BB|

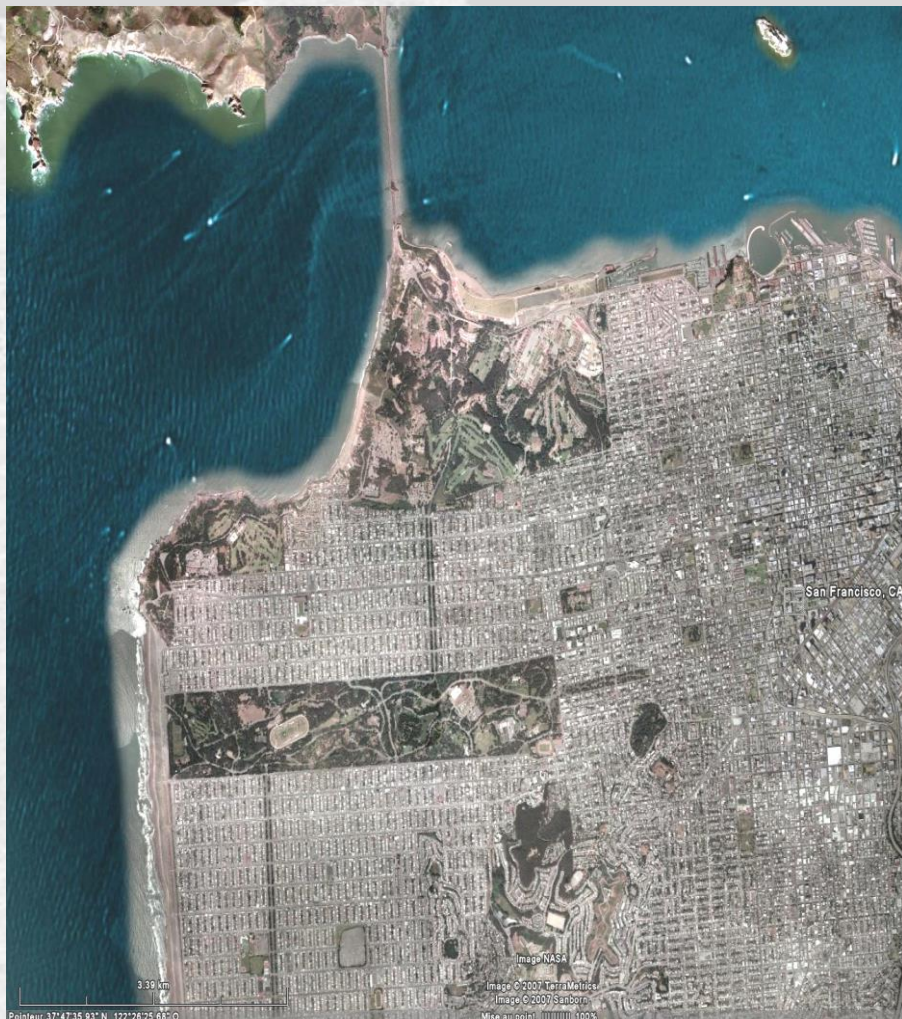
|AB|

|AA-BB|

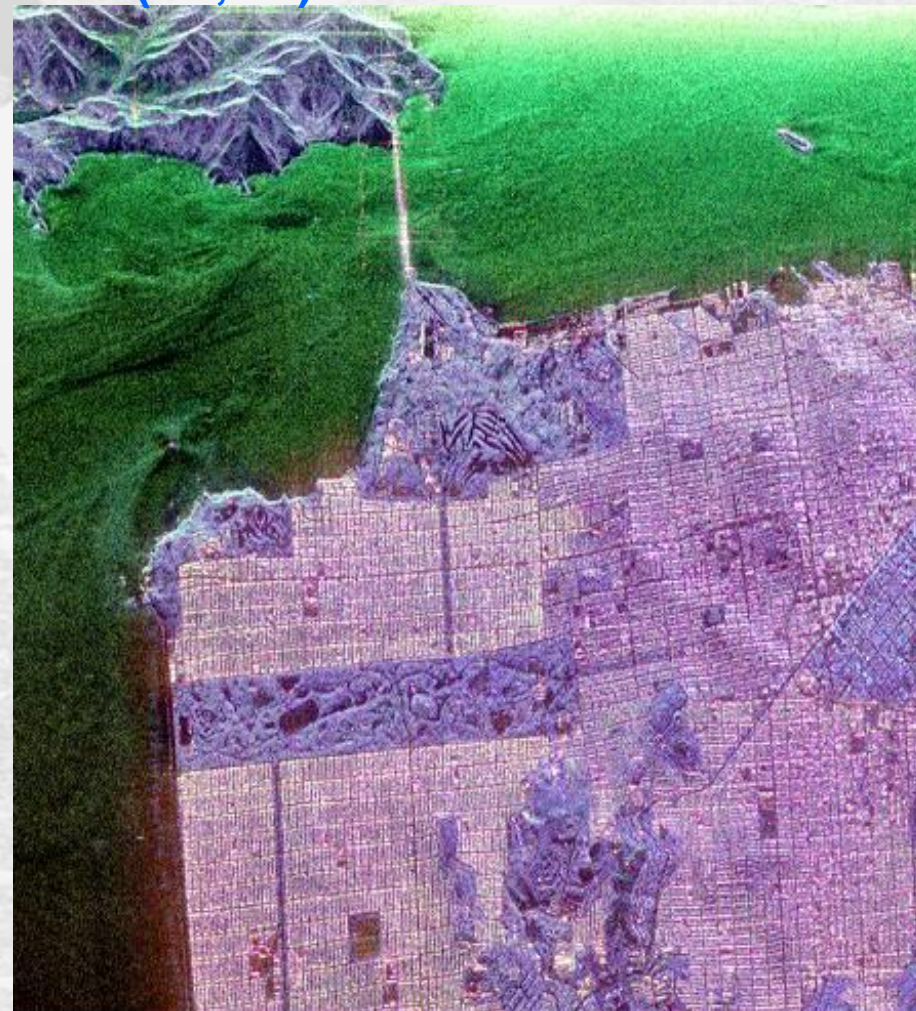
With: A=Linear +45° B=Linear -45°



## (LC,RC) POLARISATION BASIS



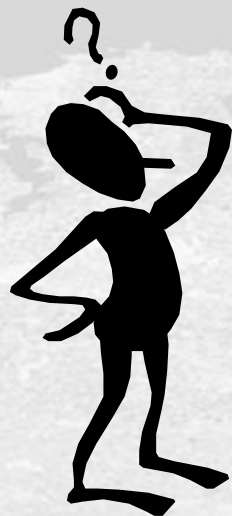
© Google Earth



|LL+RR|

|LR|

|LL-RR|



## POLARIMETRIC GOLDEN NUMBER

## POLARIMETRIC TARGET DIMENSION



$$[S] = \begin{bmatrix} S_{XX} & S_{XY} \\ S_{YX} & S_{YY} \end{bmatrix}$$

## 5 DEGREES OF FREEDOM

$$|S_{XX}|, |S_{XY}|, |S_{YY}|$$

$$\phi_{XY-XX}, \phi_{YY-XX}$$

## COHERENCY MATRIX [T]

### 9 HUYNEN REAL PARAMETERS

$$(A_0, B_0, B, C, D, E, F, G, H)$$

## TARGET MONOSTATIC POLARIMETRIC « DIMENSION »

||  
5

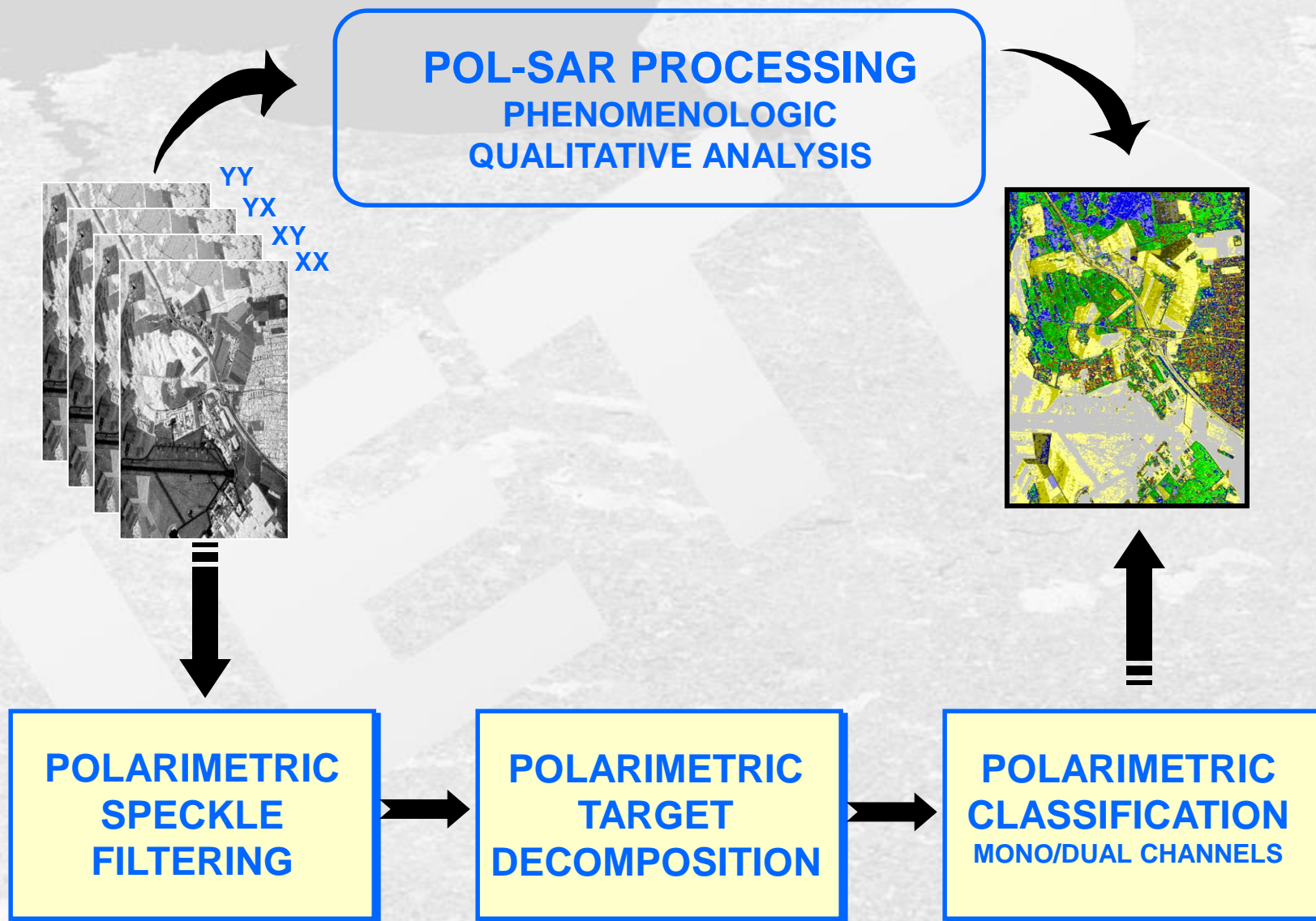
## 9 - 5 = 4 TARGET EQUATIONS

$$2A_0(B_0 + B) = C^2 + D^2$$

$$2A_0(B_0 - B) = G^2 + H^2$$

$$2A_0E = CH - DG$$

$$2A_0F = CG + DH$$



## POLARIMETRIC SPECKLE FILTERING IS NOT AN EXACT SCIENCE SUBJECTIVE, IMAGE DEPENDENT

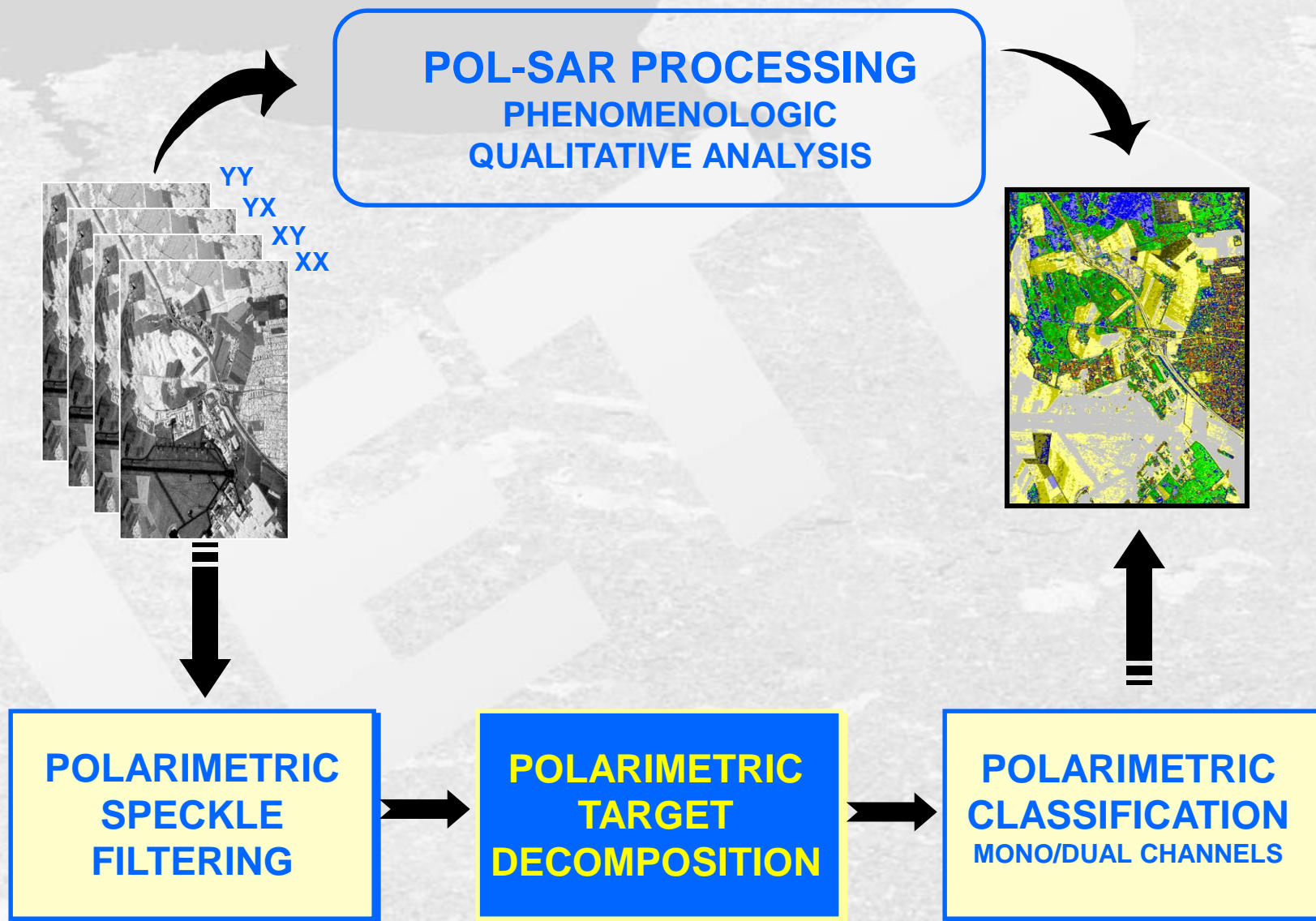
### Quantitative Criteria (J.S. Lee - IGARSS 98)

- Speckle Reduction (E.N.L)
- Edge Sharpness Preservation
- Line and Point Target Contrast Preservation
- Retention of Mean Values in Homogeneous Regions
- Retention of Texture Information
- Retention of Polarimetric Information (co, cross-correlations)
- Computational Efficiency
- Implementation Complexity

$$[\hat{T}] = E([T]) - k[E([T]) - [T]]$$

**THE POLARIMETRIC SPECKLE LEE FILTER  
IS TODAY A GOOD COMPROMISE**







$$[T] = \underline{k} \underline{k}^{*T}$$



AVERAGING DATA



SECOND ORDER STATISTICS

COHERENCY MATRICES

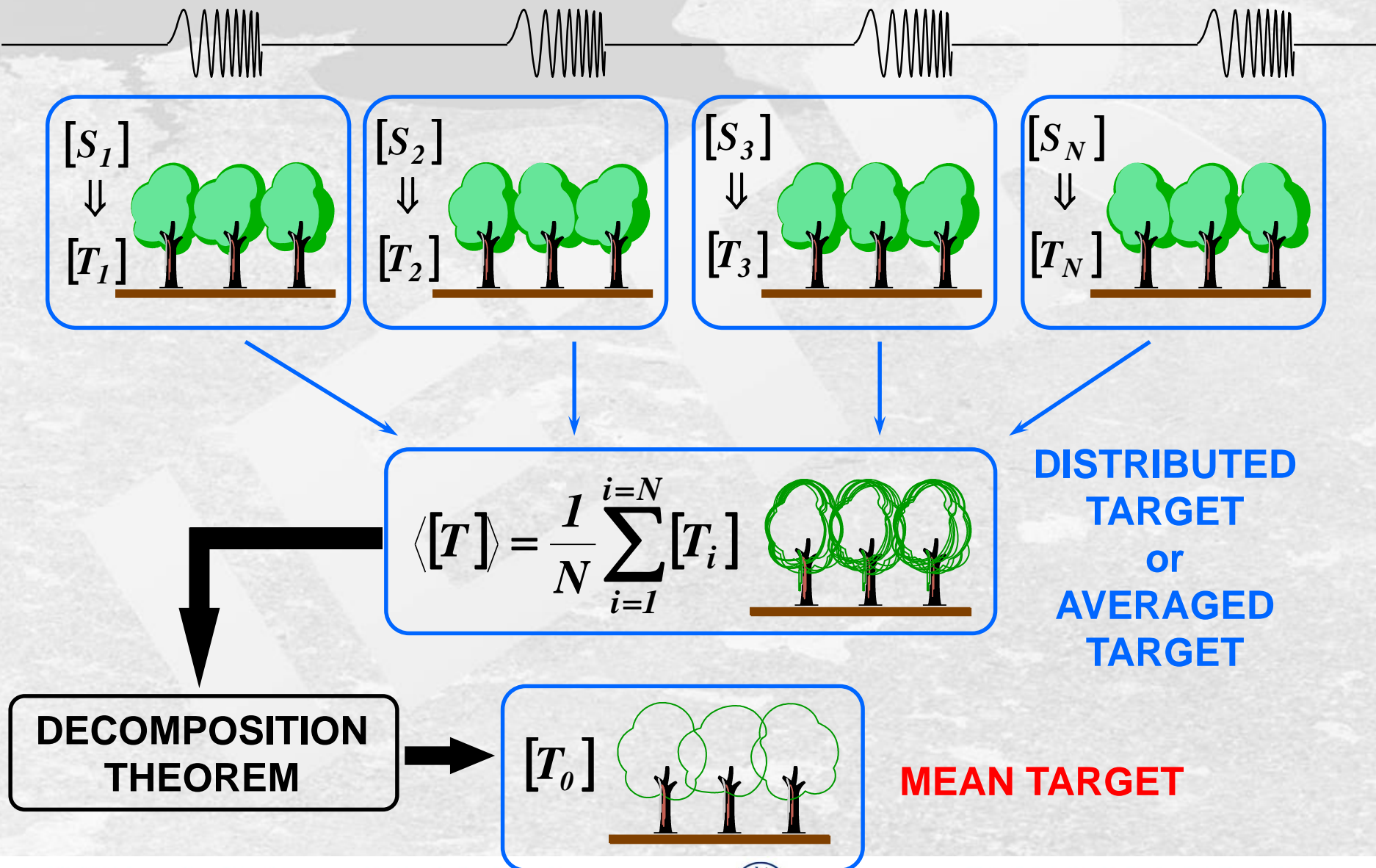
$$\langle [T] \rangle = \frac{1}{N} \sum_{i=1}^N \underline{k}_i \underline{k}_i^{*T}$$



SMOOTHING AVERAGING



CONCEPT OF THE DISTRIBUTED TARGET



[S]

[T]

[C]

**COHERENT DECOMPOSITION**

E. KROGAGER (1990)

W.L. CAMERON (1990)

[K]

**TARGET DICHOTOMY**

J.R. HUYNEN (1970)

R.M. BARNES (1988)

**EIGENVECTORS BASED DECOMPOSITION**

S.R. CLOUDE (1985)

W.A. HOLM (1988)

**EIGENVECTORS / EIGENVALUES ANALYSIS & MODEL BASED DECOMPOSITION**

J.J. VAN ZYL (1992-2008), M. ARII (2010)  
TSVM (R. TOUZI – 2007)

**EIGENVECTORS / EIGENVALUES ANALYSIS ENTROPY / ANISOTROPY**

S.R. CLOUDE - E. POTTIER (1996-1997)

**AZIMUTHAL SYMMETRY**

**MODEL BASED DECOMPOSITION**

A.J. FREEMAN – S.L. DURDEN (1992)  
Y. YAMAGUSHI (2005 - 2012), AN (2010)

# TARGET DECOMPOSITIONS



[S]

[T]

[C]

## COHERENT DECOMPOSITION

E. KROGAGER (1990)

W.L. CAMERON (1990)

[K]

## TARGET DICHOTOMY

J.R. HUYNEN (1970)

R.M. BARNES (1988)

## EIGENVECTORS BASED DECOMPOSITION

S.R. CLOUDE (1985)

W.A. HOLM (1988)

## EIGENVECTORS / EIGENVALUES ANALYSIS & MODEL BASED DECOMPOSITION

J.J. VAN ZYL (1992-2008), M. ARII (2010)  
TSVM (R. TOUZI – 2007)

## EIGENVECTORS / EIGENVALUES ANALYSIS ENTROPY / ANISOTROPY

S.R. CLOUDE - E. POTTIER (1996-1997)

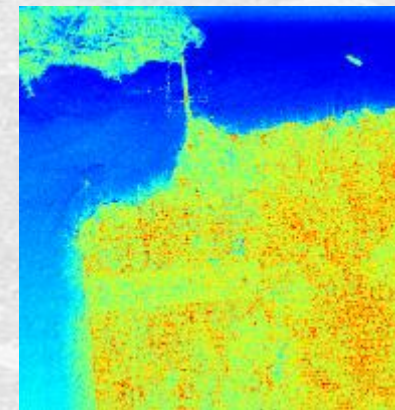
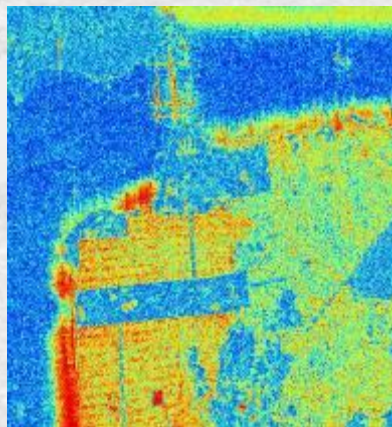
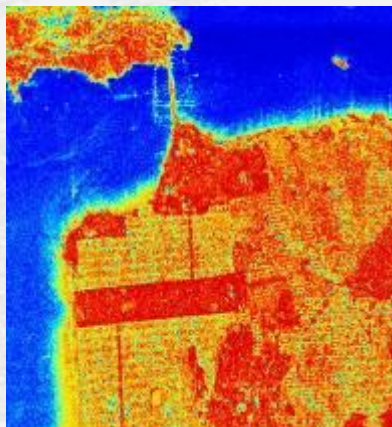
## AZIMUTHAL SYMMETRY

## MODEL BASED DECOMPOSITION

A.J. FREEMAN – S.L. DURDEN (1992)  
Y. YAMAGUSHI (2005 - 2012), AN (2010)



# THE $H/A/\alpha$ POLARIMETRIC TARGET DECOMPOSITION THEOREM



**S.R. CLOUDE - E. POTTIER (1995 - 1996)**

**TARGET VECTOR**  $\underline{k} = \frac{1}{\sqrt{2}} \begin{bmatrix} S_{XX} + S_{YY} & S_{XX} - S_{YY} & 2S_{XY} \end{bmatrix}^T$

**LOCAL ESTIMATE OF THE COHERENCY MATRIX**  $\langle [T] \rangle = \frac{1}{N} \sum_{i=1}^N \underline{k}_i \cdot \underline{k}_i^{*T} = \frac{1}{N} \sum_{i=1}^N [T_i]$


## EIGENVECTORS / EIGENVALUES ANALYSIS

$$\langle [T] \rangle = [U_3][\Sigma][U_3]^{-1} = \begin{bmatrix} \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \begin{bmatrix} \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix}^{*T}$$

**ORTHOGONAL EIGENVECTORS**

**REAL EIGENVALUES**

$$\lambda_1 > \lambda_2 > \lambda_3$$



$$P_i = \frac{\lambda_i}{\sum_{k=1}^3 \lambda_k}$$

$$\langle [T] \rangle = [U_3][\Sigma][U_3]^{-1} = \begin{bmatrix} \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \begin{bmatrix} \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix}^{*T}$$

ORTHOGONAL  
EIGENVECTORS

REAL EIGENVALUES

$$\lambda_1 > \lambda_2 > \lambda_3$$



## PARAMETERISATION OF THE SU(3) UNITARY MATRIX

$$[U_3] = \begin{bmatrix} \cos \alpha_1 e^{j\phi_1} & & \\ \sin \alpha_1 \cos \beta_1 e^{j\phi_1} e^{j\delta_1} & \cos \alpha_2 e^{j\phi_2} & \\ \sin \alpha_1 \sin \beta_1 e^{j\phi_1} e^{j\gamma_1} & \sin \alpha_2 \cos \beta_2 e^{j\phi_2} e^{j\delta_2} & \cos \alpha_3 e^{j\phi_3} \\ & \sin \alpha_2 \sin \beta_2 e^{j\phi_2} e^{j\gamma_2} & \sin \alpha_3 \cos \beta_3 e^{j\phi_3} e^{j\delta_3} \\ & & \sin \alpha_3 \sin \beta_3 e^{j\phi_3} e^{j\gamma_3} \end{bmatrix}$$

TARGET 1

TARGET 2

TARGET 3



## PROBABILITIES

$$P_i = \frac{\lambda_i}{\sum_{k=1}^3 \lambda_k}$$



## AVERAGED PARAMETERS

$$\begin{aligned} \underline{\alpha} &= P_1 \alpha_1 + P_2 \alpha_2 + P_3 \alpha_3 & \underline{\beta} &= P_1 \beta_1 + P_2 \beta_2 + P_3 \beta_3 \\ \underline{\gamma} &= P_1 \gamma_1 + P_2 \gamma_2 + P_3 \gamma_3 & \underline{\delta} &= P_1 \delta_1 + P_2 \delta_2 + P_3 \delta_3 \end{aligned}$$

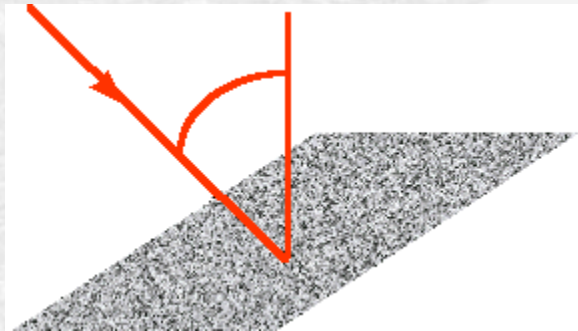


## UNITARY TARGET VECTOR ( $\underline{u}_0$ ) OF THE MEAN DOMINANT MECHANISM

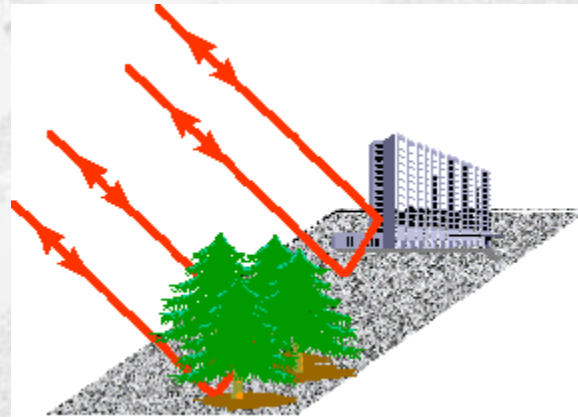
$$\underline{u}_0 = \left[ \cos(\underline{\alpha}) \quad \sin(\underline{\alpha}) \cos(\underline{\beta}) e^{j\underline{\delta}} \quad \sin(\underline{\alpha}) \sin(\underline{\beta}) e^{j\underline{\gamma}} \right]^T$$

## $\alpha$ PHYSICAL INTERPRETATION

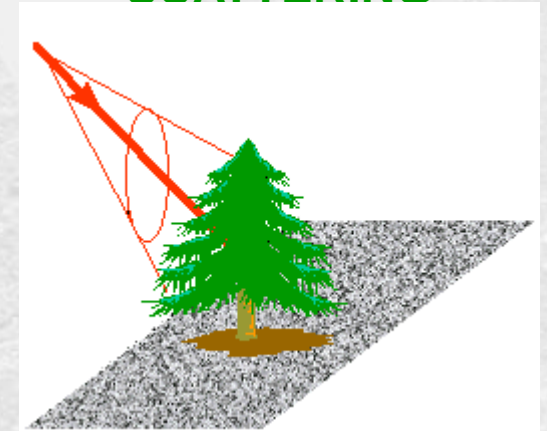
### SINGLE BOUNCE SCATTERING (ROUGH SURFACE)



### DOUBLE BOUNCE SCATTERING



### VOLUME SCATTERING



$$a \mapsto b \Rightarrow v \mapsto 0$$



$$\alpha \mapsto 0$$

$$a \mapsto -b \Rightarrow \varepsilon \mapsto 0$$

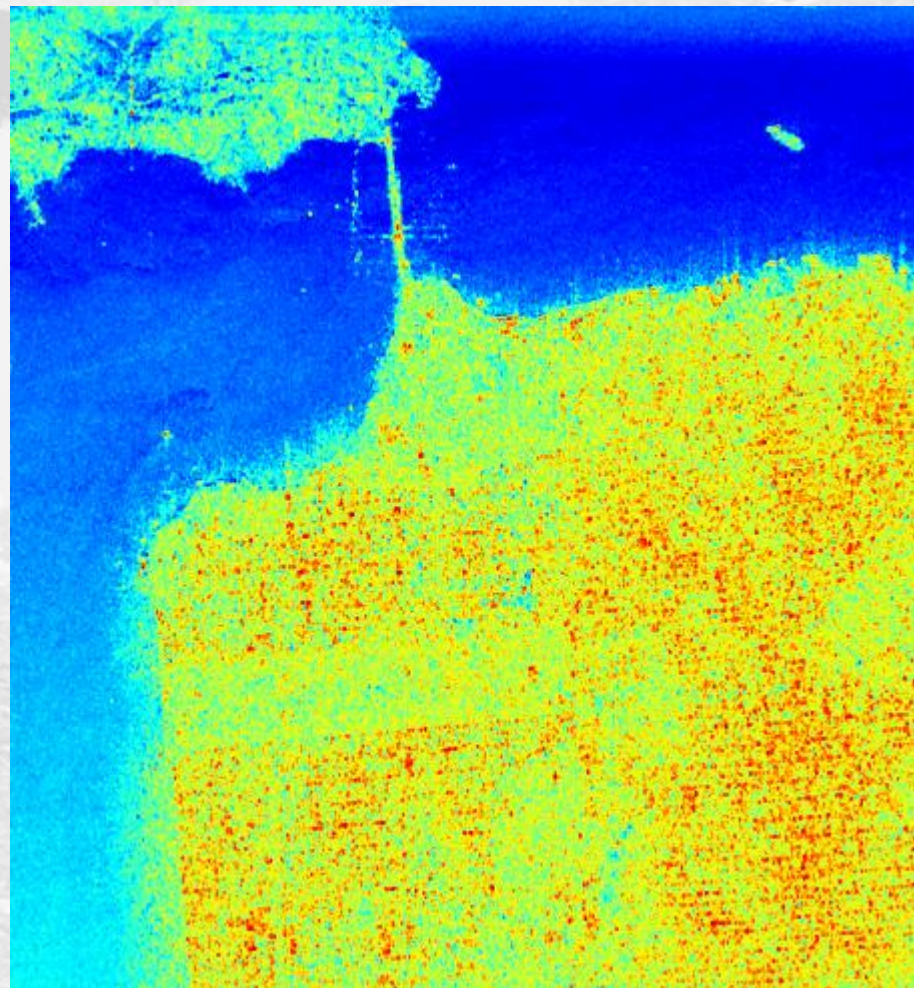


$$\alpha \mapsto \frac{\pi}{2}$$

$$a \gg b \Rightarrow \varepsilon \approx v$$



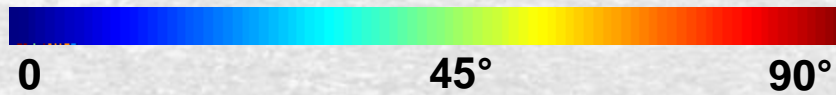
$$\alpha \mapsto \frac{\pi}{4}$$



$2A_0$

$B_0 + B$

$B_0 - B$



EIGENVALUES  $\lambda_1 \lambda_2 \lambda_3$  : ROLL INVARIANT

PROBABILITIES  $P_1 P_2 P_3$  : ROLL INVARIANT



## ENTROPY

(DEGREE OF RANDOMNESS  
STATISTICAL DISORDER)

$$H = - \sum_{i=1}^3 P_i \log_3(P_i)$$



### PURE TARGET

$$\lambda_1 = \text{SPAN} \quad \lambda_2 = 0 \quad \lambda_3 = 0$$

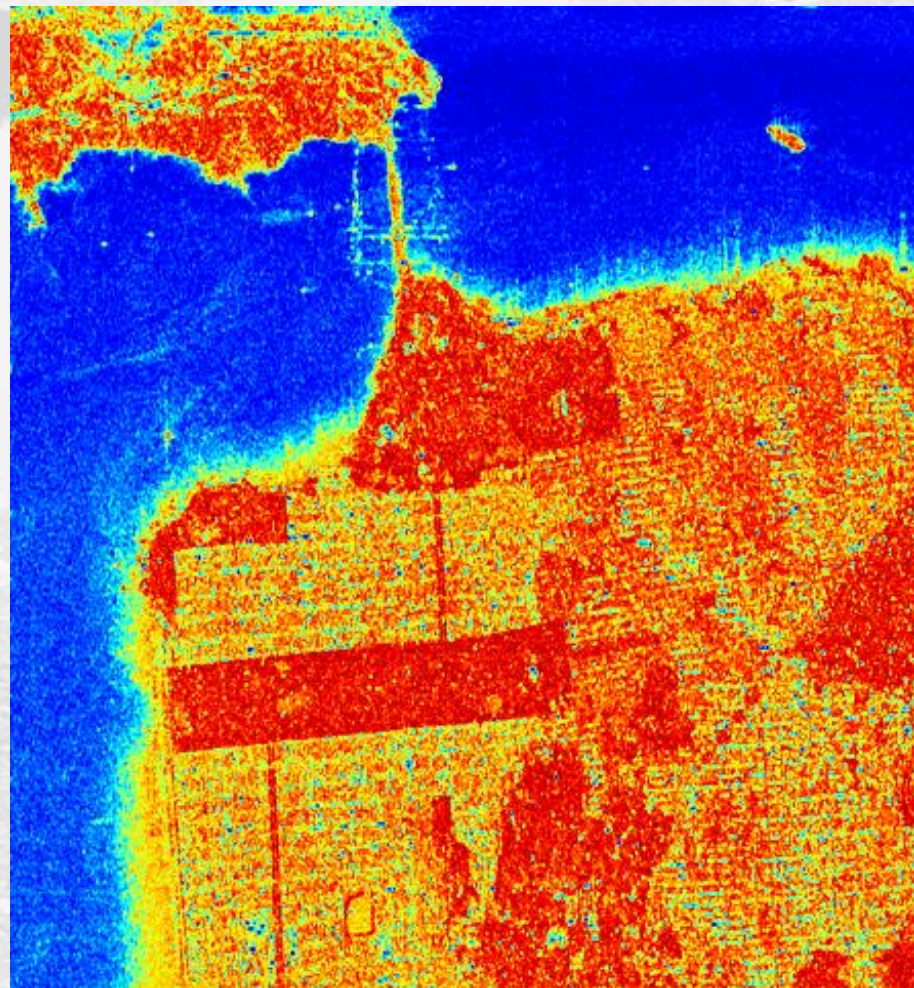
$$H = 0$$



### DISTRIBUTED TARGET

$$\lambda_1 = \lambda_2 = \lambda_3 = \text{SPAN} / 3$$

$$H = 1$$



$2A_0$

$B_0 + B$

$B_0 - B$



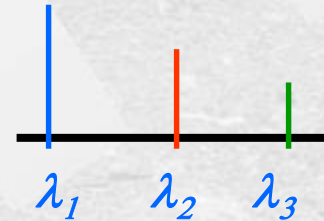
ENTROPY (H)

DIFFICULT MECHANISM DISCRIMINATION WHEN :  $H > 0.7$



**ANISOTROPY**  
(EIGENVALUES SPECTRUM)

$$A = \frac{\lambda_2 - \lambda_3}{\lambda_2 + \lambda_3}$$



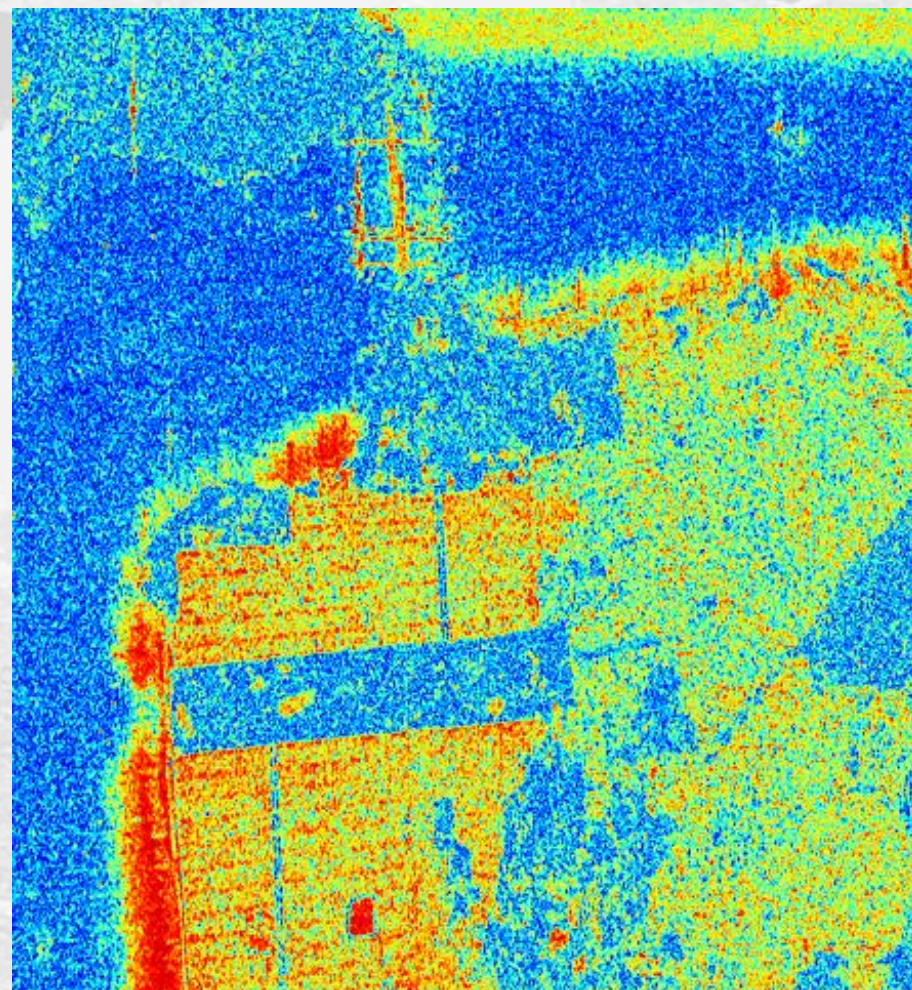
**COMPLEMENTARY TO ENTROPY**



**DISCRIMINATION WHEN  $H > 0.7$**



**ROLL INVARIANT**



$2A_0$

$B_0 + B$

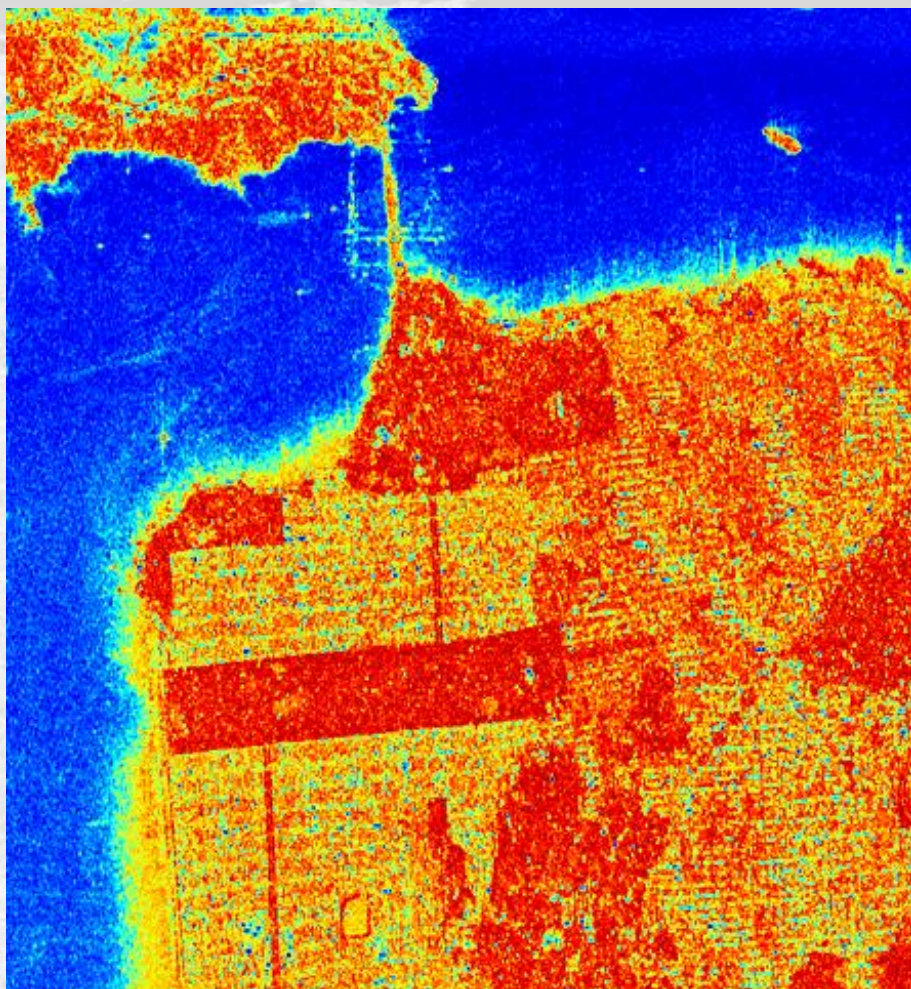
$B_0 - B$

0

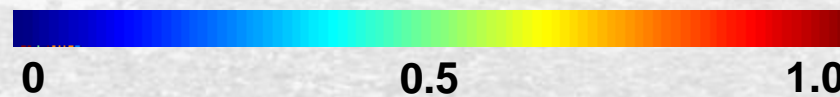
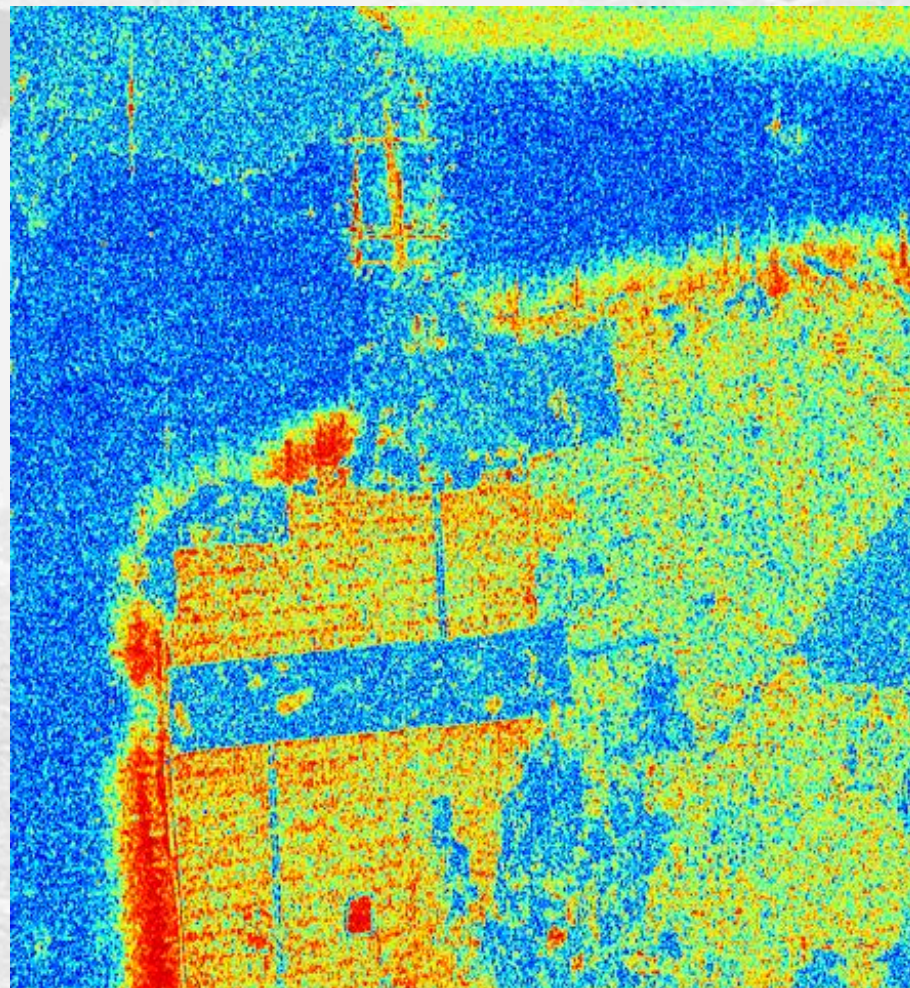
0.5

1.0

ANISOTROPY (A)



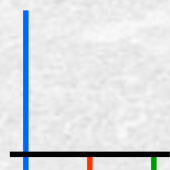
ENTROPY (H)



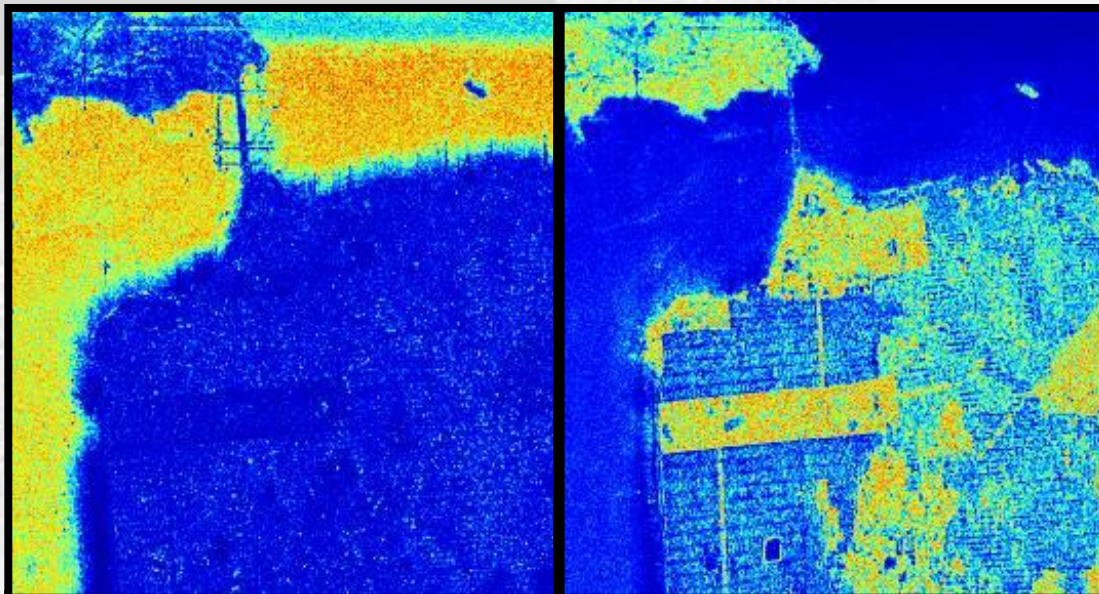
ANISOTROPY (A)



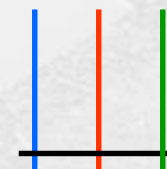
$(1-H)(1-A)$



1 MECHANISM

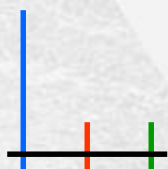


H(1-A)

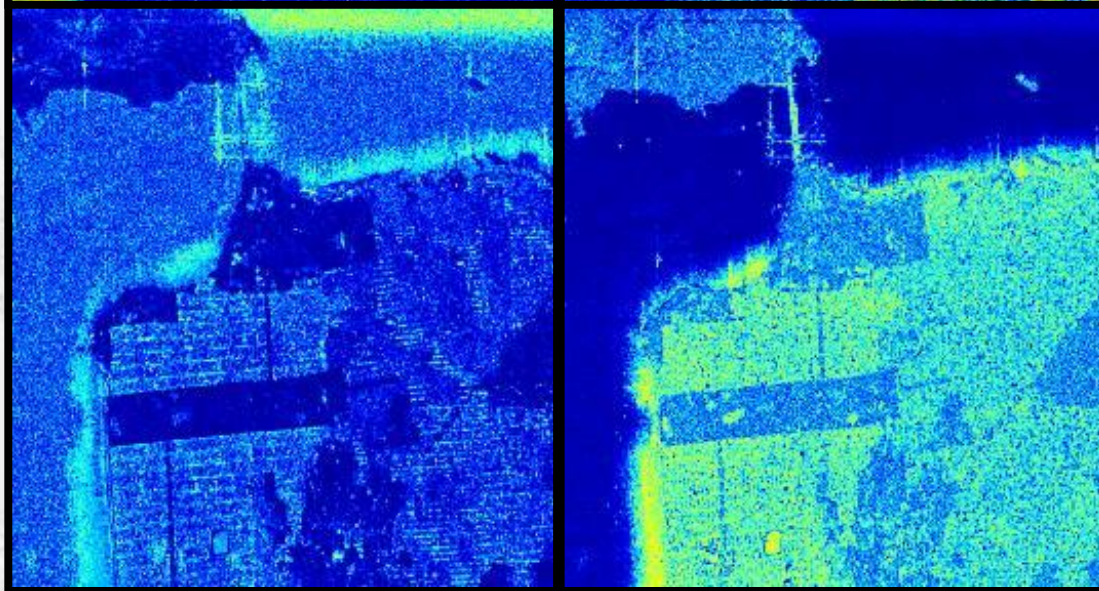


3 MECHANISMS

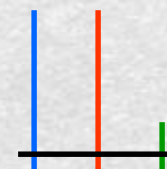
A(1-H)



2 MECHANISMS



HA



2 MECHANISMS



0

0.25



0.5

[S]

[T]

[C]

**COHERENT DECOMPOSITION**

E. KROGAGER (1990)

W.L. CAMERON (1990)

[K]

**TARGET DICHOTOMY**

J.R. HUYNEN (1970)

R.M. BARNES (1988)

**EIGENVECTORS BASED DECOMPOSITION**

S.R. CLOUDE (1985)

W.A. HOLM (1988)

**EIGENVECTORS / EIGENVALUES ANALYSIS & MODEL BASED DECOMPOSITION**

J.J. VAN ZYL (1992-2008), M. ARII (2010)  
TSVM (R. TOUZI – 2007)

**EIGENVECTORS / EIGENVALUES ANALYSIS ENTROPY / ANISOTROPY**

S.R. CLOUDE - E. POTTIER (1996-1997)

**AZIMUTHAL SYMMETRY**

**MODEL BASED DECOMPOSITION**

A.J. FREEMAN – S.L. DURDEN (1992)  
Y. YAMAGUSHI (2005 - 2012), AN (2010)

## MODEL BASED

## DECOMPOSITIONS

➔ **A. FREEMAN – S. DURDEN**  
(1992)



➔ **Y. YAMAGUCHI – S. SINGH**  
(2005 - 2018)



➔ **And others ...**  
(2015 - 2017)



# TARGET DECOMPOSITION FOR TARGETS WITH REFLECTION SYMMETRY

MODEL BASED DECOMPOSITION

A. FREEMAN – S. DURDEN (1992)



*A. Freeman and S.L. Durden, "A Three-Component Scattering Model for Polarimetric SAR Data"  
IEEE TGRS, vol. 36, no. 3, May 1998*

## 3 COMPONENTS SCATTERING MECHANISM MODEL

$$\langle [T] \rangle = [T_S] + [T_D] + [T_V]$$



**SINGLE  
SCATTERING**

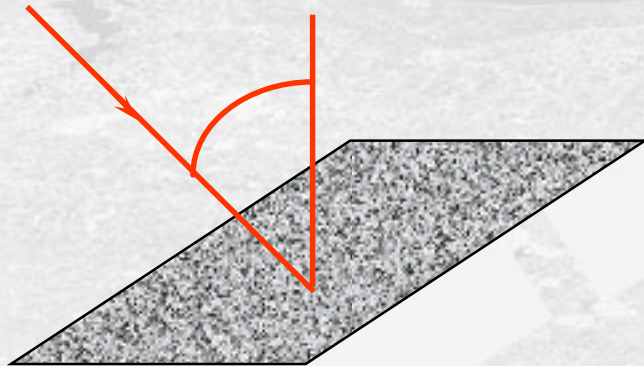


**DOUBLE  
SCATTERING**



**VOLUME  
SCATTERING**

## SINGLE SCATTERING (ROUGH SURFACE)



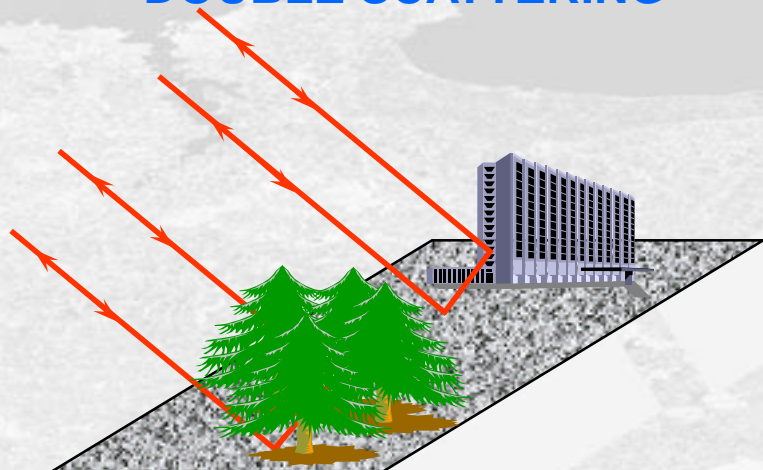
### MECHANISM

$$[S_s] = \begin{bmatrix} R_H & 0 \\ 0 & R_V \end{bmatrix} \Rightarrow \underline{k}_s = \begin{bmatrix} R_H + R_V \\ R_H - R_V \\ 0 \end{bmatrix}$$

### COHERENCY MATRIX

$$[T_s] = f_s \begin{bmatrix} |\beta+1|^2 & (\beta+1)(\beta-1)^* & 0 \\ (\beta+1)^*(\beta-1) & |\beta-1|^2 & 0 \\ 0 & 0 & 0 \end{bmatrix} \quad \begin{aligned} f_s &= |R_V|^2 \\ \beta &= \frac{R_H}{R_V} \end{aligned}$$

## DOUBLE SCATTERING



## MECHANISM

$$[S_D] = \begin{bmatrix} R_{GH} R_{TH} & 0 \\ 0 & -R_{GV} R_{TV} \end{bmatrix}$$

$$\Rightarrow \underline{k}_D = \begin{bmatrix} R_{GH} R_{TH} - R_{GV} R_{TV} \\ R_{GH} R_{TH} + R_{GV} R_{TV} \\ 0 \end{bmatrix}$$

## COHERENCY MATRIX

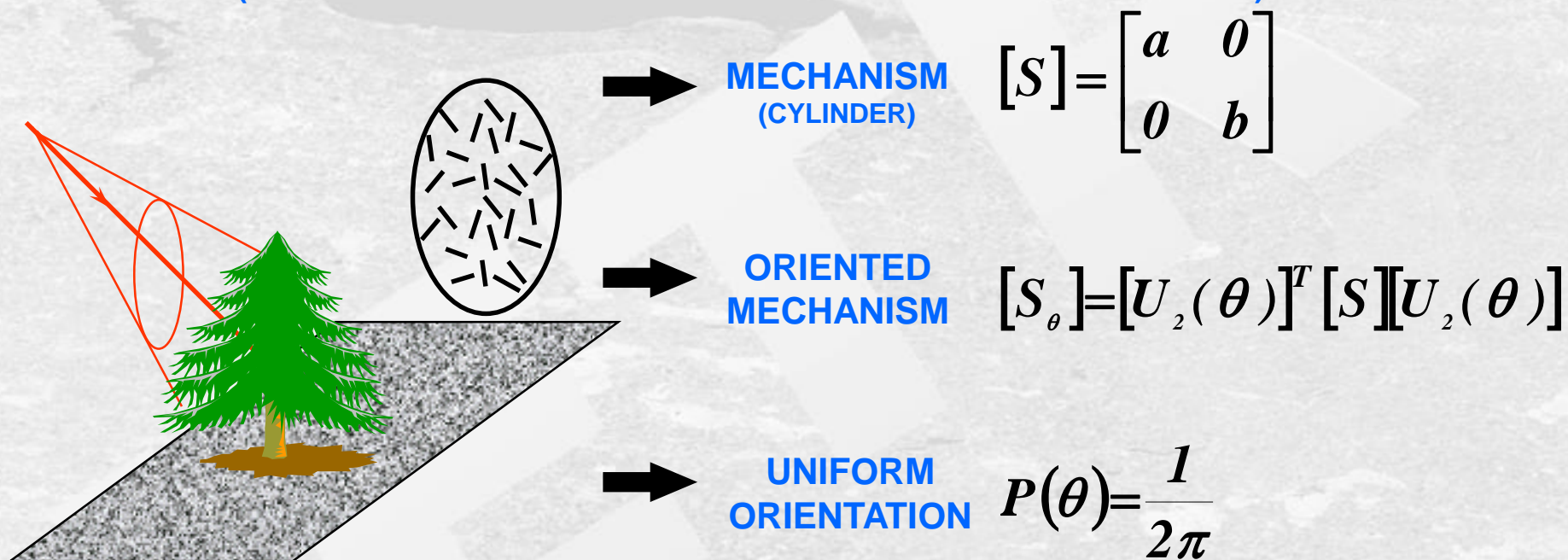
$$[T_D] = f_D \begin{bmatrix} |\alpha - 1|^2 & (\alpha - 1)(\alpha + 1)^* & 0 \\ (\alpha - 1)^* (\alpha + 1) & |\alpha + 1|^2 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$f_D = |R_{GV} R_{TV}|^2$$

$$\alpha = \frac{R_{GH} R_{TH}}{R_{GV} R_{TV}}$$

## VOLUME SCATTERING

(RANDOMLY ORIENTED VERY THIN CYLINDER-LIKE SCATTERERS)



**SECOND-ORDER STATISTICS**

$$[T_v] = \langle [T_\theta] \rangle = \int_0^{2\pi} [T_v] P(\theta) d\theta$$

**COVARIANCE MATRIX**

(THIN CYLINDERS)

$$[T_v] = \frac{f_v}{3} \begin{bmatrix} 4 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$

$a \mapsto 1 \quad b \mapsto 0$



## 3 COMPONENTS SCATTERING MECHANISM MODEL

$$\langle [T] \rangle = [T_S] + [T_D] + [T_V]$$



**SINGLE  
SCATTERING**



**DOUBLE  
SCATTERING**



**VOLUME  
SCATTERING**

$$T_{11} = f_S |\beta + 1|^2 + f_D |\alpha - 1|^2 + \frac{4f_V}{3}$$

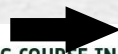
$$T_{12} = f_S (\beta + 1)(\beta - 1)^* + f_D (\alpha - 1)(\alpha + 1)^*$$

$$T_{22} = f_S |\beta - 1|^2 + f_D |\alpha + 1|^2 + \frac{2f_V}{3}$$

$$T_{33} = \frac{2f_V}{3}$$



**5 UNKNOWN REAL COEFFICIENTS**



**4 OBSERVED EQUATIONS**

$$\text{if } \Re\left(\langle S_{XX} S_{YY}^* \rangle - \frac{f_V}{3}\right) \geq 0 \Rightarrow \alpha = +1$$

$$\text{if } \Re\left(\langle S_{XX} S_{YY}^* \rangle - \frac{f_V}{3}\right) \leq 0 \Rightarrow \beta = +1$$



$$\{f_S, |\beta|, f_D, |\alpha|, f_V\}$$

$$\text{span} = \langle T_{11} \rangle + \langle T_{22} \rangle + \langle T_{33} \rangle = f_S (1 + \beta^2) + f_D (1 + |\alpha|^2) + \frac{2}{3} f_V$$



**SINGLE BOUNCE  
SCATTERING  
(ODD)**



**DOUBLE DOUBLE  
SCATTERING  
(DBL)**



**VOLUME  
SCATTERING  
(VOL)**



$$2A_0$$

$$B_0 + B$$

$$B_0 - B$$



$$ODD = f_s (1 + \beta^2)$$

$$VOL = \frac{2f_v}{\beta}$$

$$DBL = f_D (1 + \alpha^2)$$

# TARGET DECOMPOSITION FOR TARGETS WITHOUT REFLECTION SYMMETRY

MODEL BASED - 4 COMPONENTS DECOMPOSITION

Y. YAMAGUCHI et al. (2005 - 2013)



## MEDIUM WITHOUT ANY REFLECTION SYMMETRY

### 4 COMPONENTS SCATTERING MECHANISM MODEL

$$\langle [T] \rangle = [T_S] + [T_D] + [T_V] + [T_H]$$



**SINGLE  
SCATTERING**



**DOUBLE  
SCATTERING**



**VOLUME  
SCATTERING**



**HELIX  
SCATTERING**

$$[S]_{\pm Helix} = \frac{1}{2} \begin{bmatrix} 1 & \pm j \\ \pm j & -1 \end{bmatrix}$$

$$\langle [T] \rangle_{Helix} = \frac{1}{2} \left\langle \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & \pm j \\ 0 & \mp j & 1 \end{bmatrix} \right\rangle$$

**Non reflection  
Symmetric cases**

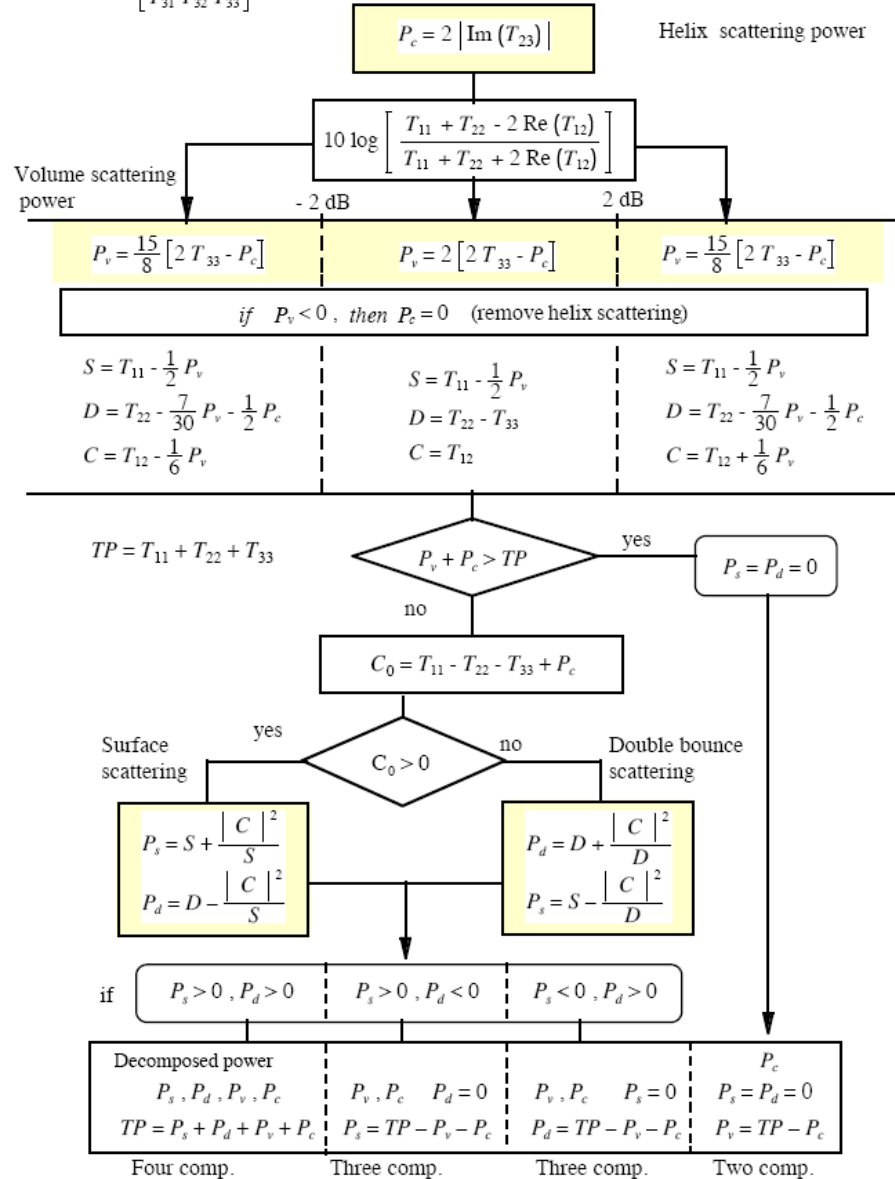
Yamaguchi Y., Moriyama T., Ishido M. and Yamada H., "Four-Component Scattering Model for Polarimetric SAR Image Decomposition", IEEE Trans. Geos. Remote Sens., vol. 43, no. 8, August 2005.

Yamaguchi Y., Yajima Y. and Yamada H., "A Four-Component Decomposition of POLSAR Images Based on the Coherency Matrix", IEEE Geos. Rem. Sens. Letters, vol. 3, no. 3, July 2006.

# MODEL BASED DECOMPOSITION

Y40

$$\langle [T] \rangle = \begin{bmatrix} T_{11} & T_{12} & T_{13} \\ T_{21} & T_{22} & T_{23} \\ T_{31} & T_{32} & T_{33} \end{bmatrix} = \frac{1}{n} \sum^n k_p k_p^\dagger$$





$$2A_0$$

$$B_0 + B$$

$$B_0 - B$$

$$ODD = f_s (1 + \beta^2)$$

$$VOL = \frac{2f_v}{\beta}$$

$$DBL = f_D (1 + \alpha^2)$$

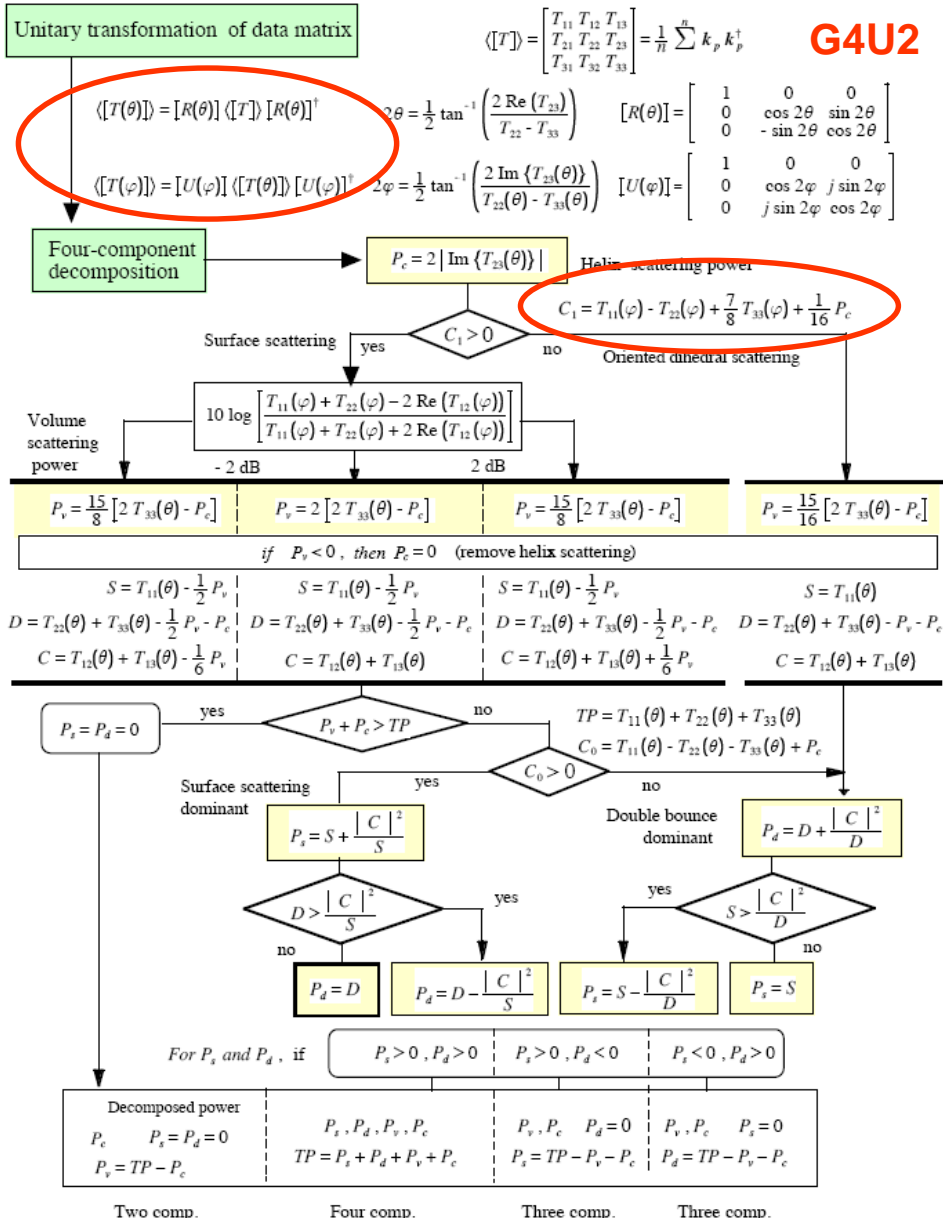
Y. Yamaguchi, A. Sato, W.M. Boerner, R. Sato, H. Yamada, “*4-component scattering power decomposition with rotation of coherency matrix*”, IEEE TGRS vol. 49, no. 6, **June 2011**.

A. Sato, Y. Yamaguchi, G. Singh, and S.-E. Park, “*4-component scattering power decomposition with extended volume scattering model*”, IEEE GRS Letters, vol. 9, no. 2, pp. 166–170, **March 2012**.

G. Singh, Y. Yamaguchi, S.E. Park, Y. Cui, H. Kobayashi, « *Hybrid Freeman/Eigenvalue Decomposition Method With Extended Volume Scattering Model* » IEEE GRS Letters, vol. 10, no. 1, **January 2013**.

G. Singh, Y. Yamaguchi, S.E. Park, « *General Four-Component Scattering Power Decomposition With Unitary Transformation of Coherency Matrix* » IEEE TGRS vol. 51, no. 5, **May 2013**.







$2A_0$

$B_0 + B$

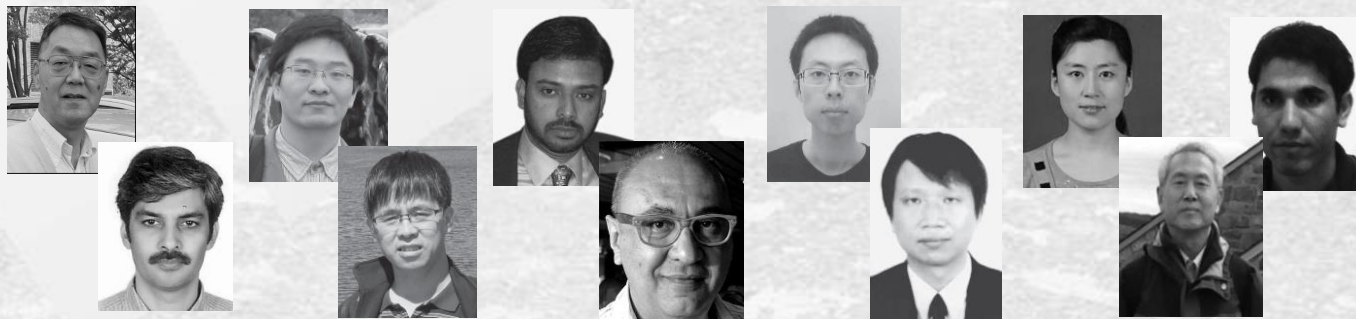
$B_0 - B$



$ODD$   $DBL$   $VOL$

# TARGET DECOMPOSITION FOR TARGETS WITHOUT REFLECTION SYMMETRY

MODEL BASED - 4 / 5 / 6 COMPONENTS DECOMPOSITION  
(2015 - 2017)



A. BHATTACHARYA, A. FRERY, “*Modifying the Yamaguchi 4-component decomposition scattering powers using a stochastic distance*”, IEEE JSTARS, vol. 8, pp 3497-3506, **July 2015**.

F. XU, Y.Q. JIN, “*Deorientation theory of Polarimetric scattering targets and application to terrain surface classification*”, IEEE TGRS Vol 43, n° 10, **October 2015**.

B. ZOU, D. LU, L. ZHANG, W.M. Moon, « *Eigen-decomposition-based Four Component Decomposition for PoSAR Data*”. IEEE JSTARS, vol. 9, pp 1286-1296, **March 2016**.

H. AGHABABAEI, M. Reza SAHEBI, “*Incoherent Target Scattering Decomposition of Polarimetric SAR Data Based on Vector Model Roll-Invariant Parameters*”. IEEE TGRS, vol. 54, no 8, **August 2016**.

G. SINGH, Y. YAMAGUCHI, “*Model-based Six-Component Scattering Matrix Power Decomposition*”, IEEE TGRS Vol 56, n° 10, **October 2018**.



$2A_0$

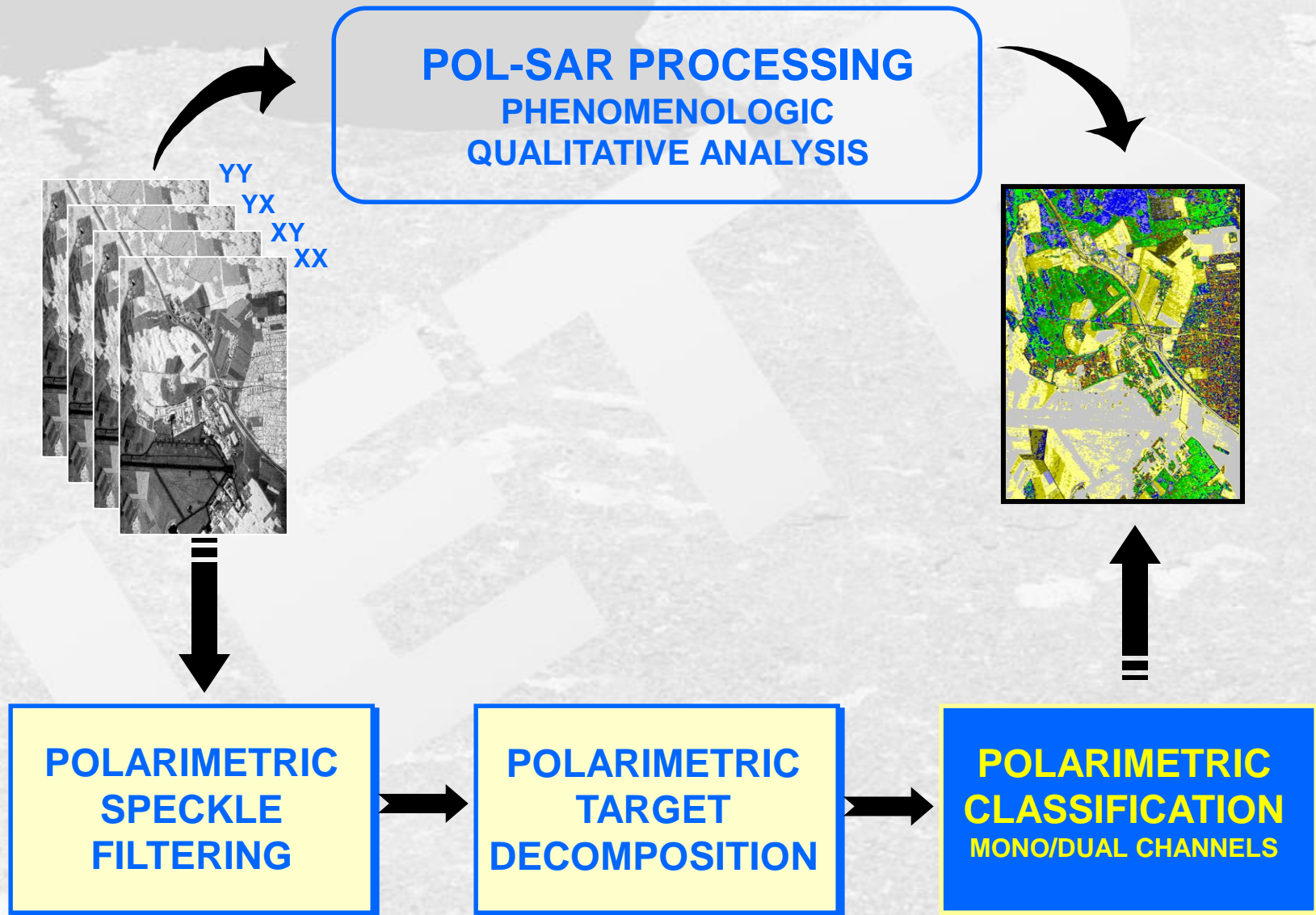
$B_0 + B$

$B_0 - B$



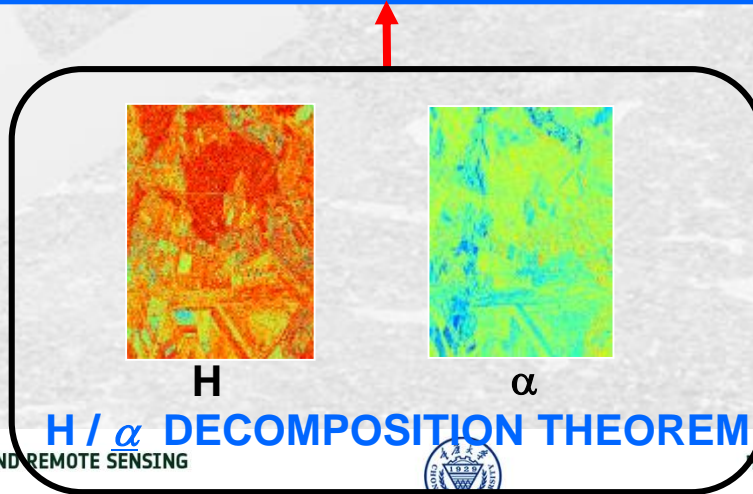
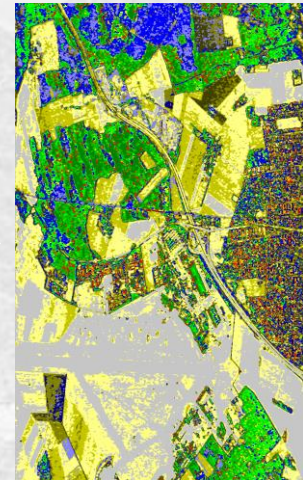
$ODD$   $DBL$   $VOL$

**Singh decomposition – 6 components**





**UNSUPERVISED  
POLAR  
CLASSIFICATION**  
S.R. CLOUDE, E.POTTIER (1996)



## ENTROPY

$$H = -\sum_{i=1}^3 P_i \log_3(P_i)$$

## $\alpha$ PARAMETER

$$\alpha = P_1\alpha_1 + P_2\alpha_2 + P_3\alpha_3$$

## ANISOTROPY

$$A = \frac{\lambda_2 - \lambda_3}{\lambda_2 + \lambda_3}$$



**3 ROLL INVARIANT PARAMETERS**

$$\underline{I} = \begin{bmatrix} \alpha \\ HA \\ H(1-A) \\ (1-H)A \\ (1-H)(1-A) \end{bmatrix}$$



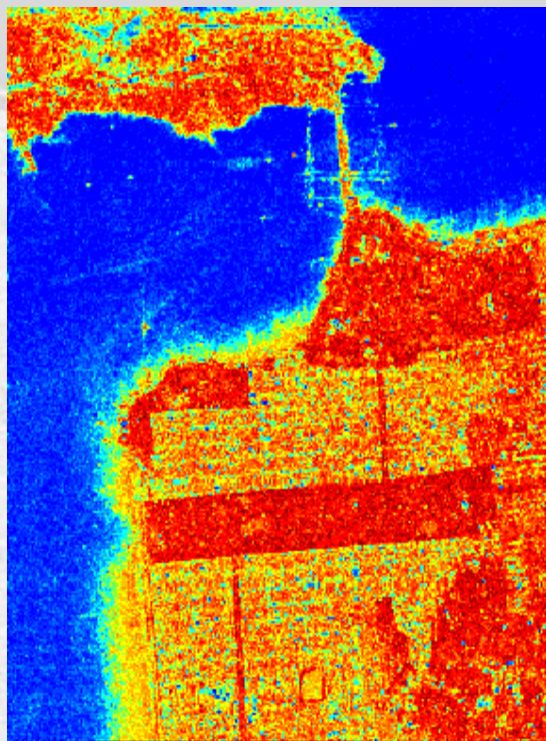
**PHYSICAL SCATTERING MECHANISM**



**TYPE OF SCATTERING PROCESS**

**SEGMENTATION / CLASSIFICATION**

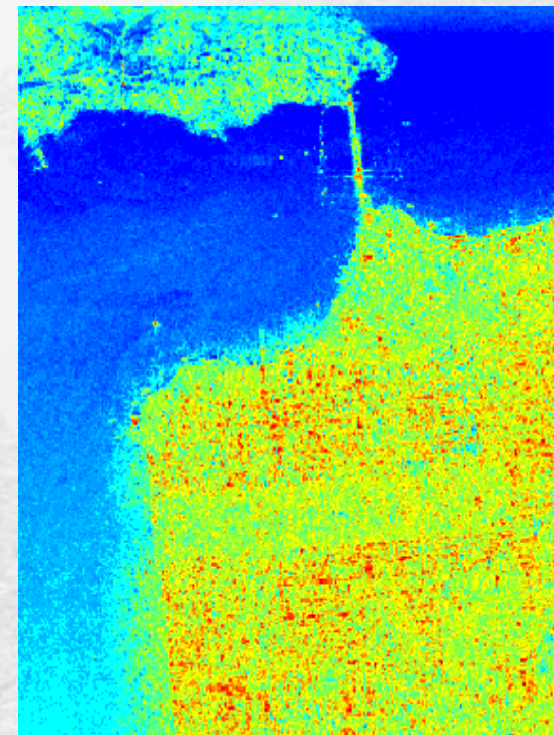




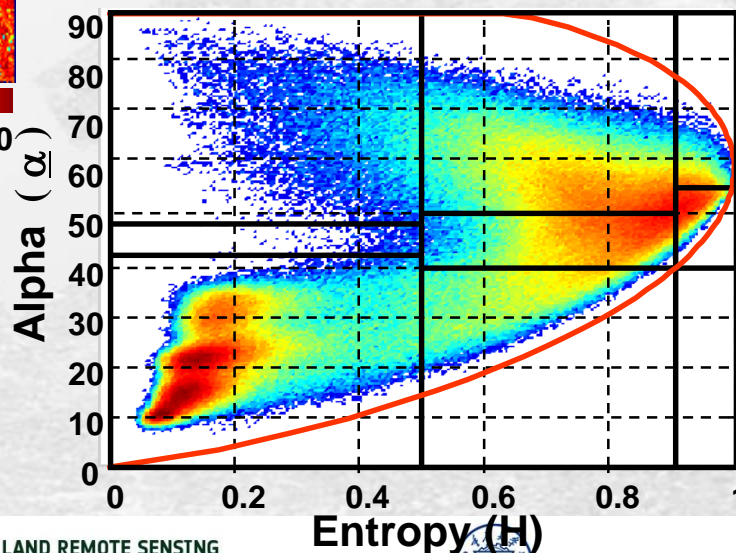
0 0.5 1.0  
H



POLSAR DATA  
DISTRIBUTION  
IN THE  
H /  $\alpha$  PLANE

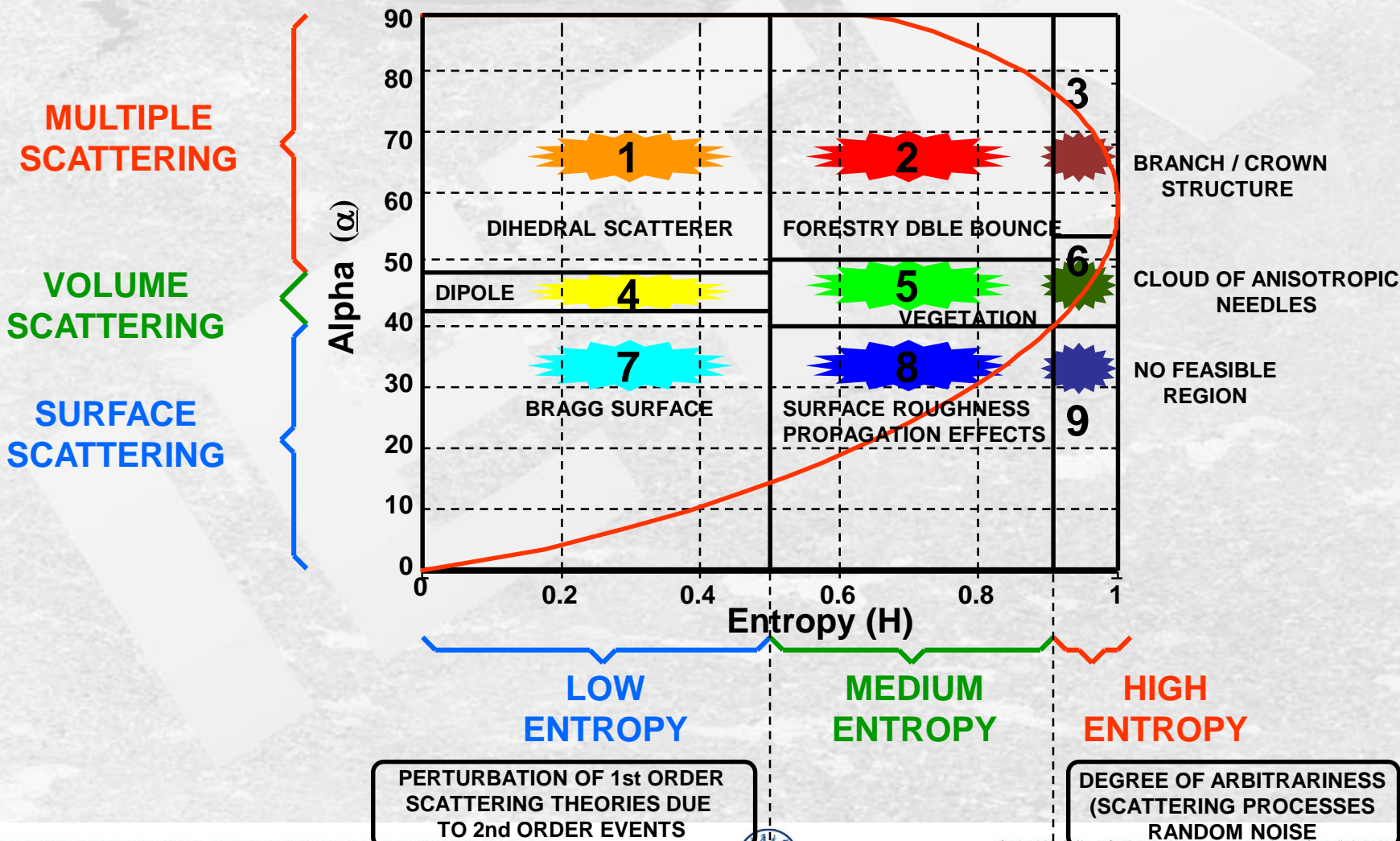


0 45° 90°  
 $\alpha$

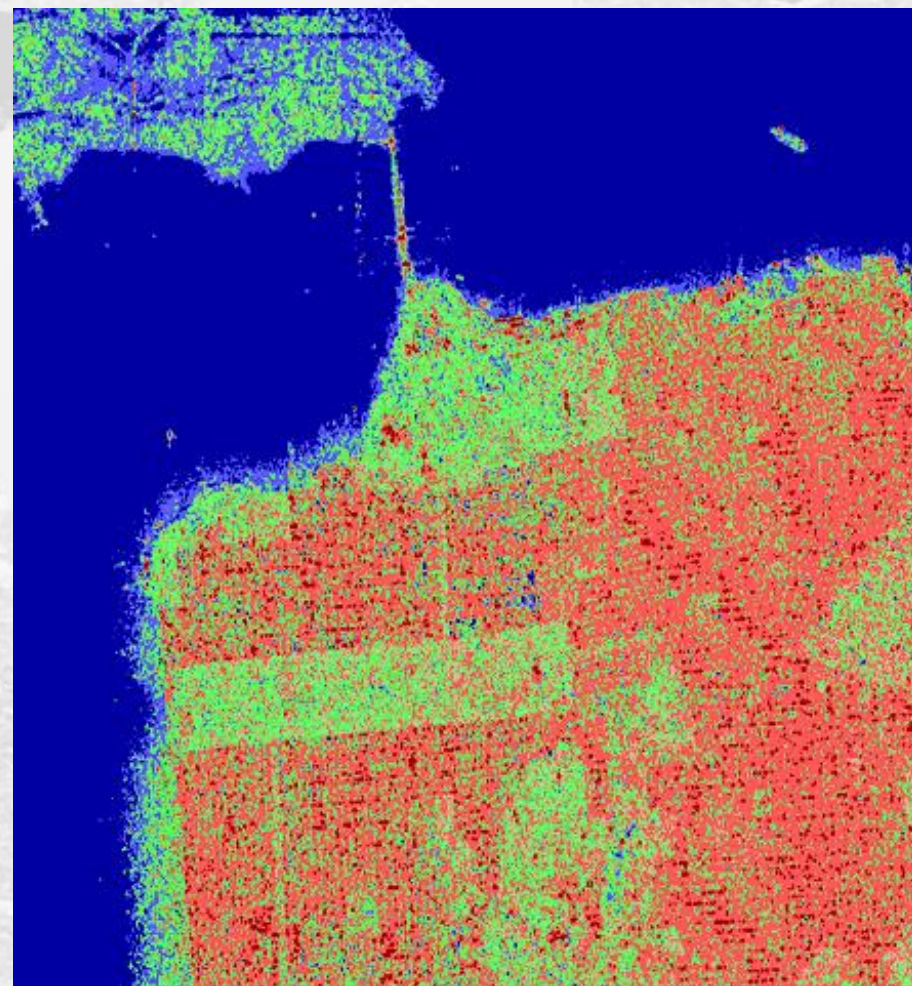


Entropy (H)

## SEGMENTATION OF THE H / $\alpha$ SPACE



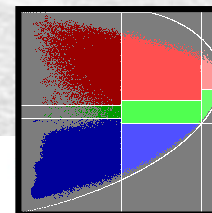
## H - $\alpha$ classification



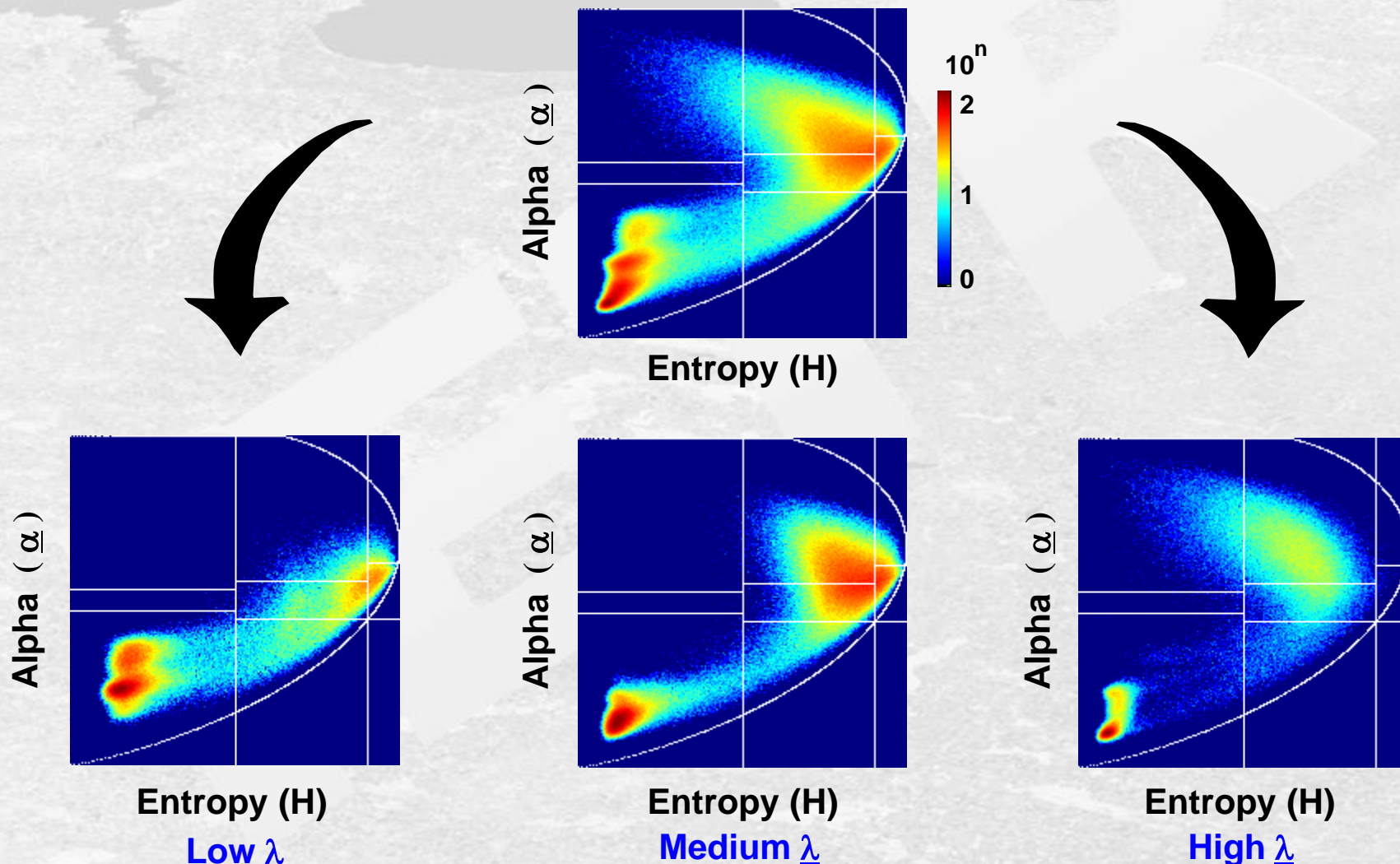
$2A_0$

$B_0 + B$

$B_0 - B$

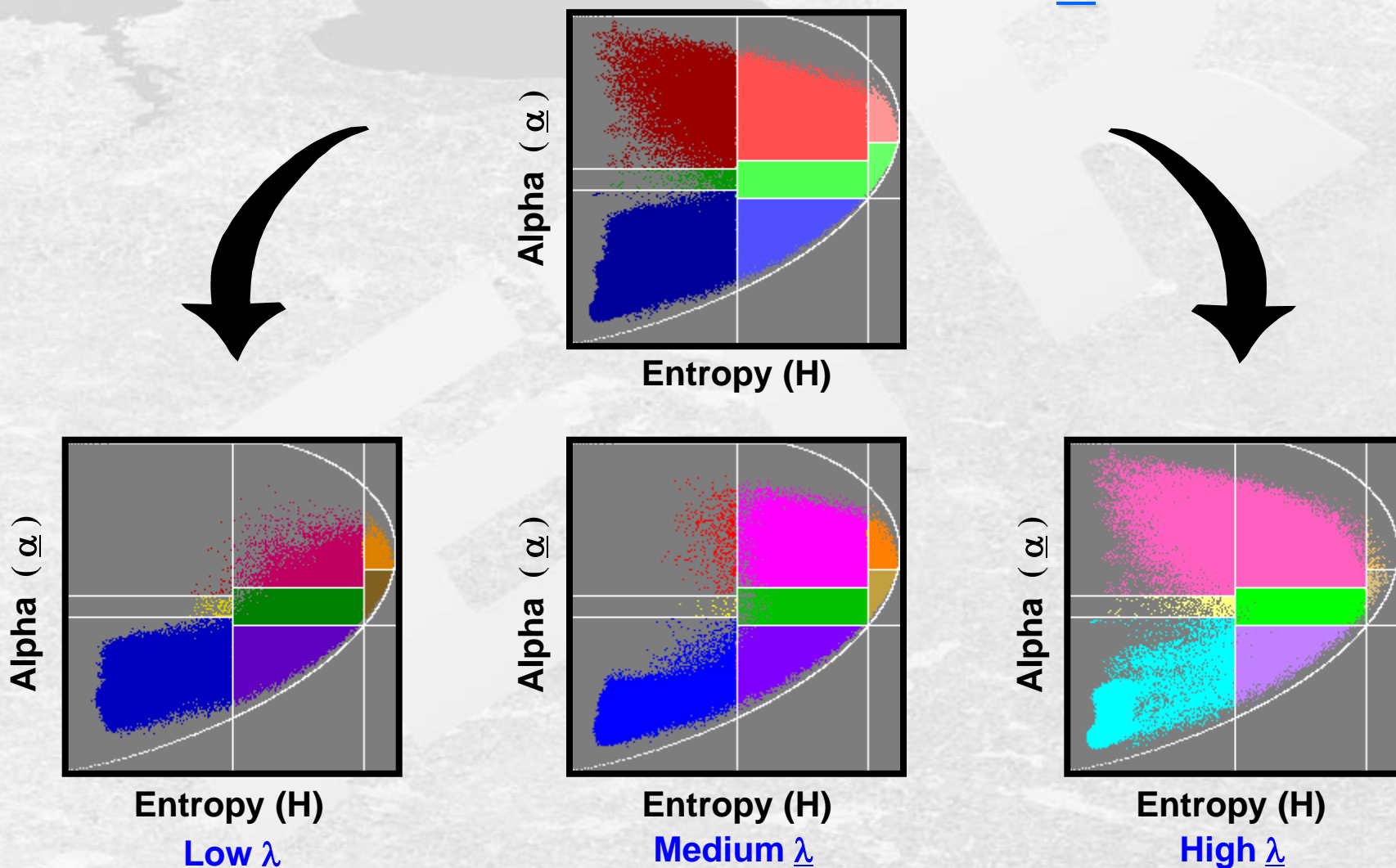


## POLSAR DATA DISTRIBUTION IN THE H / $\alpha$ PLANE



Cao Fang, Hong Wen A New Classification Method Based on Cloude-Pottier Eigenvalue / Eigenvector Decomposition, IGARSS 05, Seoul, Korea

## POLSAR DATA DISTRIBUTION IN THE H / $\alpha$ PLANE



Cao Fang, Hong Wen A New Classification Method Based on Cloude-Pottier Eigenvalue / Eigenvector Decomposition, IGARSS 05, Seoul, Korea

## H - $\alpha$ ( $\lambda$ ) classification



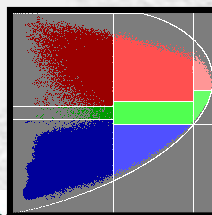
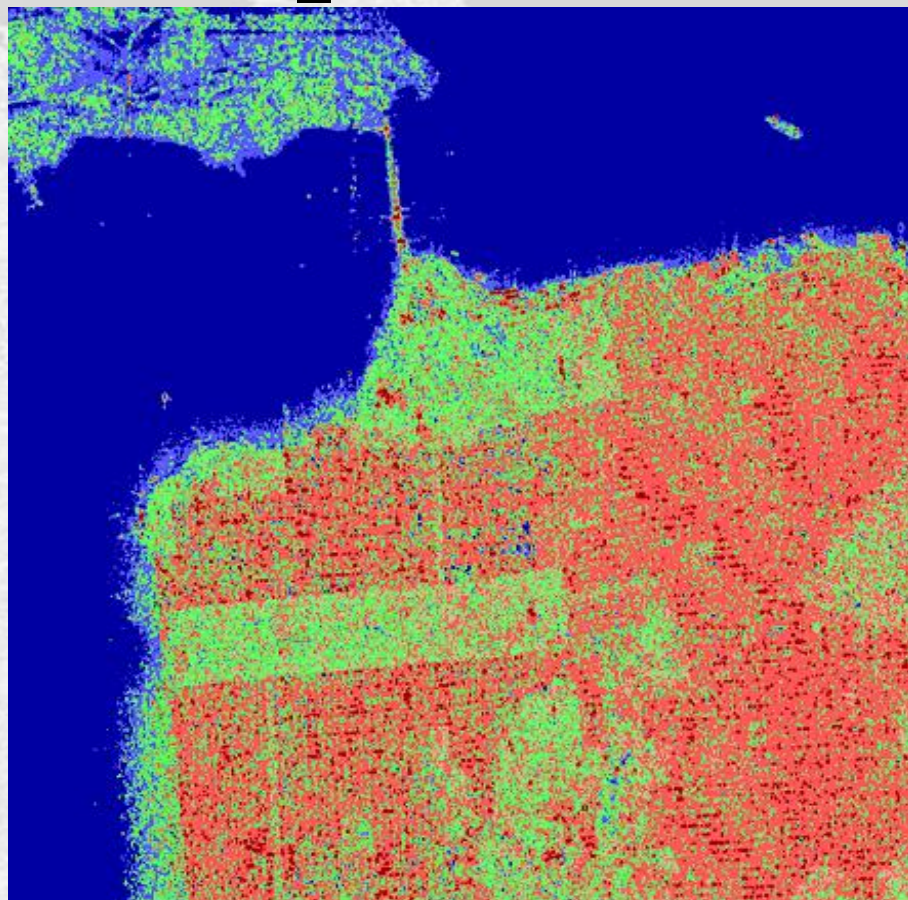
$2A_0$

$B_0 + B$

$B_0 - B$



## H- $\alpha$ classification



**H /  $\alpha$  Classification Space**  
**Sub-divided into 9 basic zones**



**Location of the boundaries**  
**is arbitrary and generically**

**Degree of arbitrariness on the**  
**setting of these boundaries**

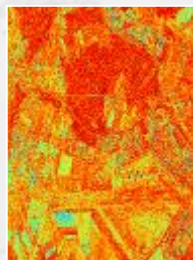
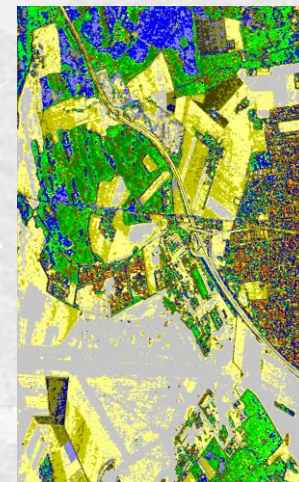


**Segmentation is offered merely**  
**to illustrate the unsupervised**  
**classification strategy and to**  
**emphasize the geometrical**  
**segmentation of physical scattering**  
**processes**

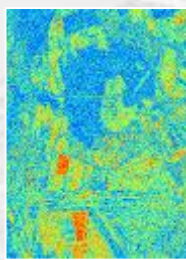
**WISHART PDF**  $P(\langle [T] \rangle / [T_m]) = \frac{L^p \langle [T] \rangle^{L-p} e^{-LTr([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$



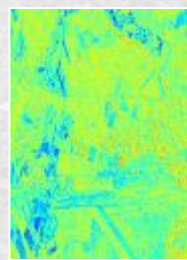
**UNSUPERVISED  
POLSAR  
CLASSIFICATION**  
E.POTTIER, J.S LEE (2000)



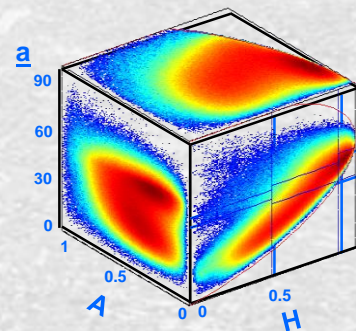
H



A



α





## PoISAR TERRAIN and LAND-USE CLASSIFICATION

**J.S. Lee, M.R. Grunes, E. Pottier, L. Ferro-Famil, “Unsupervised terrain classification preserving scattering characteristics,” *IEEE Transactions on Geoscience and Remote Sensing*, vol. 42, no.4, pp. 722-731, April, 2004.**

**J.S. Lee, M. R. Grunes and E. Pottier, “Quantitative Comparison of Classification Capability: Fully polarimetric versus Dual- and Single polarization SAR,” *IEEE TGRS*, November 2002**

**E. Pottier and J.S. Lee, “Application of the «  $H / A / \alpha$  » polarimetric decomposition theorem for unsupervised classification of fully polarimetric SAR data based on the Wishart distribution” *Proceedings of EUSAR2000***

**J.S. Lee, M.R. Grunes, T.L. Ainsworth, L. Du, D.L. Schuler, and S.R. Cloude, “ Unsupervised Classification of Polarimetric SAR Imagery Based on Target Decomposition and Wishart Distribution,” *IEEE Transactions on Geoscience and Remote Sensing*, vol. 37, no. 5, 2249-2258, September 1999.**

**J.S. Lee, M. R. Grunes and R. Kwok,” Classification of Polarimetric SAR Images Based on the Complex Wishart Distribution,” *Int. J. Remote Sensing*, vol.32, No. 5, Sept. 1994.**

**J.S. Lee, E. Pottier, *Polarimetric Radar Imaging: From Basics to Applications*, Taylor & Francis/CRC, 2009**

## Target Vector

$$\underline{X} = \begin{bmatrix} S_{HH} & \sqrt{2}S_{HV} & S_{VV} \end{bmatrix}^T$$

$$P(\underline{X}) = \frac{1}{\pi^3 |C|} e^{-\underline{X}^{*T} [C]^{-1} \underline{X}}$$

$$\underline{k} = \frac{1}{\sqrt{2}} \begin{bmatrix} S_{HH} + S_{VV} & S_{HH} - S_{VV} & 2S_{HV} \end{bmatrix}^T$$

$$P(\underline{k}) = \frac{1}{\pi^3 |T|} e^{-\underline{k}^{*T} [T]^{-1} \underline{k}}$$

## Coherency Matrix

$$\langle [T] \rangle = \frac{1}{N} \sum_{i=1}^N \underline{k}_i \cdot \underline{k}_i^{*T} = \frac{1}{N} \sum_{i=1}^N [T_i]$$

$$P(\langle [T] \rangle / [T_m]) = \frac{L^{Lp} |\langle [T] \rangle|^{L-p} e^{-L \text{Tr}([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$

# COMPLEX WISHART DISTRIBUTION

L: Number of Look      p: Polarimetric Dimension

$$P(\langle [T] \rangle / [T_m]) = \frac{L^{Lp} \|\langle [T] \rangle\|^{L-p} e^{-L \text{Tr}([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$



## BAYES MAXIMUM LIKELIHOOD CLASSIFICATION PROCEDURE

$$\langle [T] \rangle \in [T_m] \quad \text{if} \quad P([T_m] / \langle [T] \rangle) \geq P([T_j] / \langle [T] \rangle) \quad \forall j \neq m$$

Applying Bayes rule  $P([T_m] / \langle [T] \rangle) = \frac{P(\langle [T] \rangle / [T_m]) P([T_m])}{P(\langle [T] \rangle)}$

It follows

$$\langle [T] \rangle \in [T_m] \quad \text{if} \quad P(\langle [T] \rangle / [T_m]) P([T_m]) \geq P(\langle [T] \rangle / [T_j]) P([T_j]) \quad \forall j \neq m$$

$[T_m]$ : Cluster Center of the class  $m$

$$P(\langle [T] \rangle / [T_m]) = \frac{L^{Lp} \|\langle [T] \rangle\|^{L-p} e^{-LTr([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$



## BAYES MAXIMUM LIKELIHOOD CLASSIFICATION PROCEDURE

$$\langle [T] \rangle \in [T_m] \quad \text{if} \quad d_m(\langle [T] \rangle) < d_j(\langle [T] \rangle) \quad \forall j \neq m$$

with

$$d_m(\langle [T] \rangle) = LTr([T_m]^{-1} \langle [T] \rangle) + L \ln([T_m]) - \ln(P([T_m])) + K$$

$[T_m]$  : Cluster Center of the class  $m$

## ROBUSTENESS OF WISHART CLASSIFIER

$$d_m(\langle [T] \rangle) = L \text{Tr}([T_m]^{-1} \langle [T] \rangle) + L \ln([T_m]) - \ln(P([T_m])) + K$$

INDEPENDENT OF # OF LOOKS

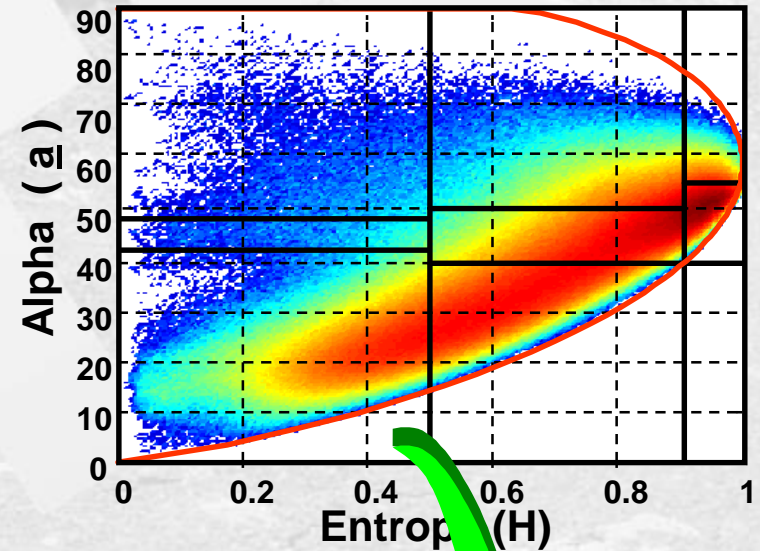
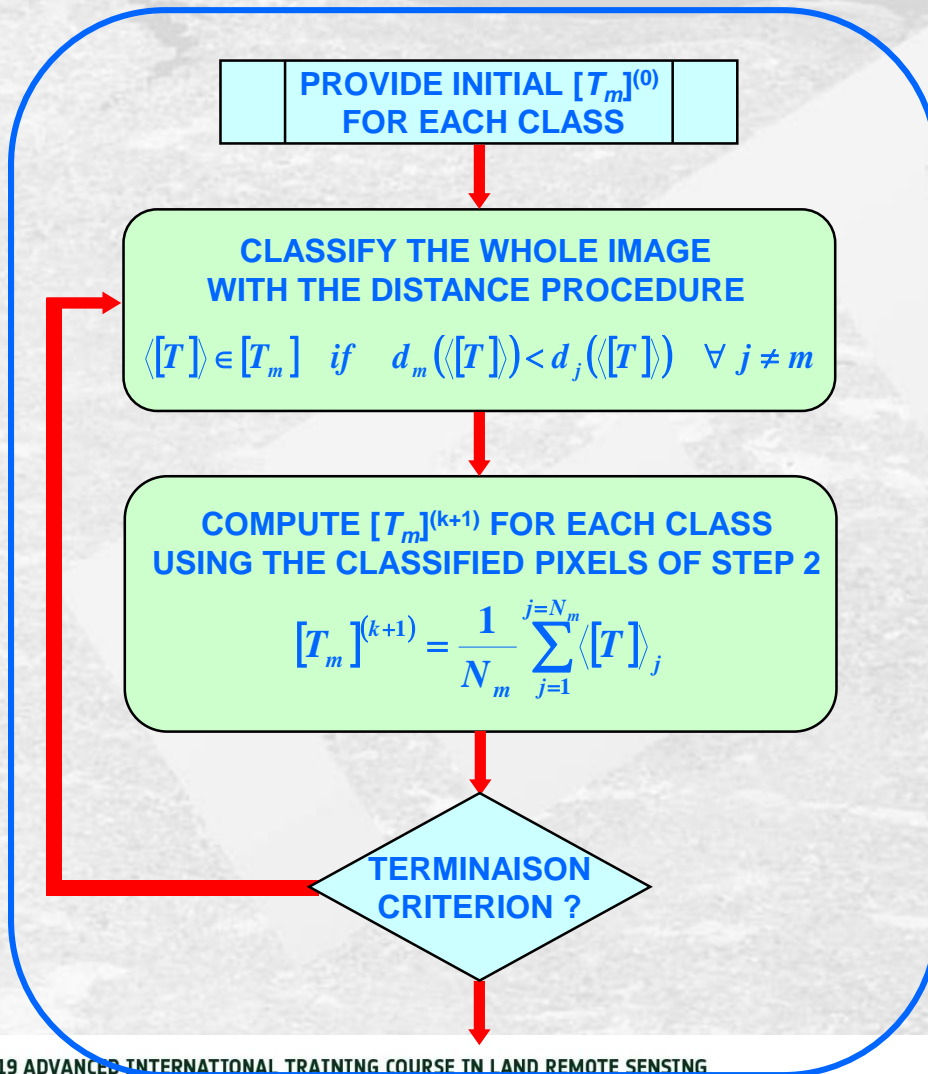
INDEPENDENT OF POLARIZATION BASIS

[T] or [C] IDENTICAL CLASSIFICATION RESULTS

For Dual-Pol ( $p=2$ ), PolSAR ( $p=3$ ), Pol-InSAR ( $p=6$ )

J.S. Lee, E. Pottier, *Polarimetric Radar Imaging: From Basics to Applications*, Taylor & Francis/CRC, 2009

## k - mean CLASSIFICATION PROCEDURE



$$[T_m]^{(0)} = \frac{1}{N_m} \sum_{k=1}^{k=N_m} \langle [T] \rangle_k$$

Cluster Center of the class  $m$   
(Lee 1998)

SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

4th ITERATION



$2A_0$

$B_0 + B$

$B_0 - B$

C1

C2

C3

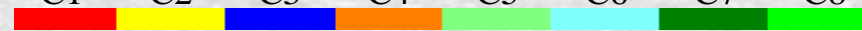
C4

C5

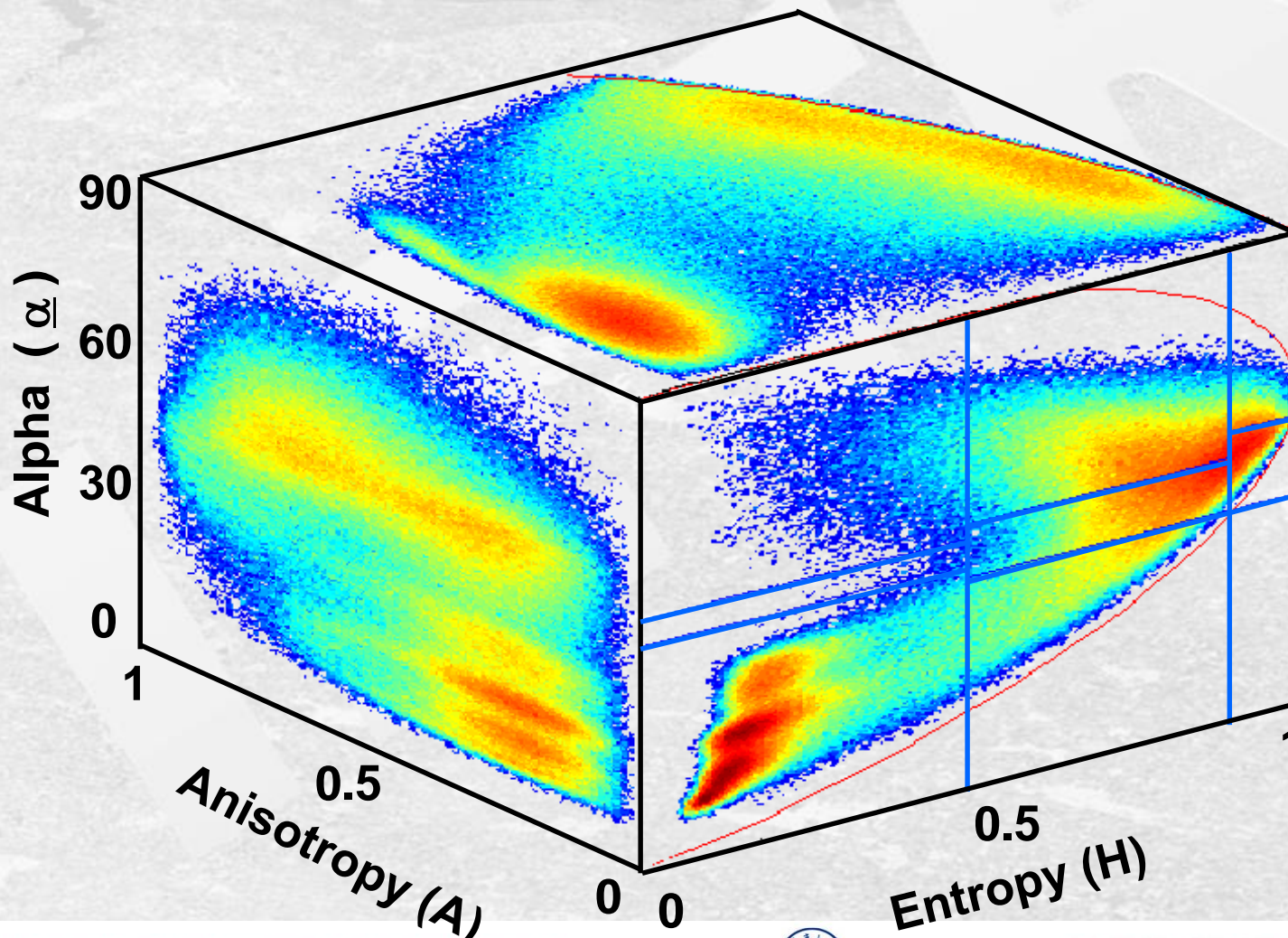
C6

C7

C8

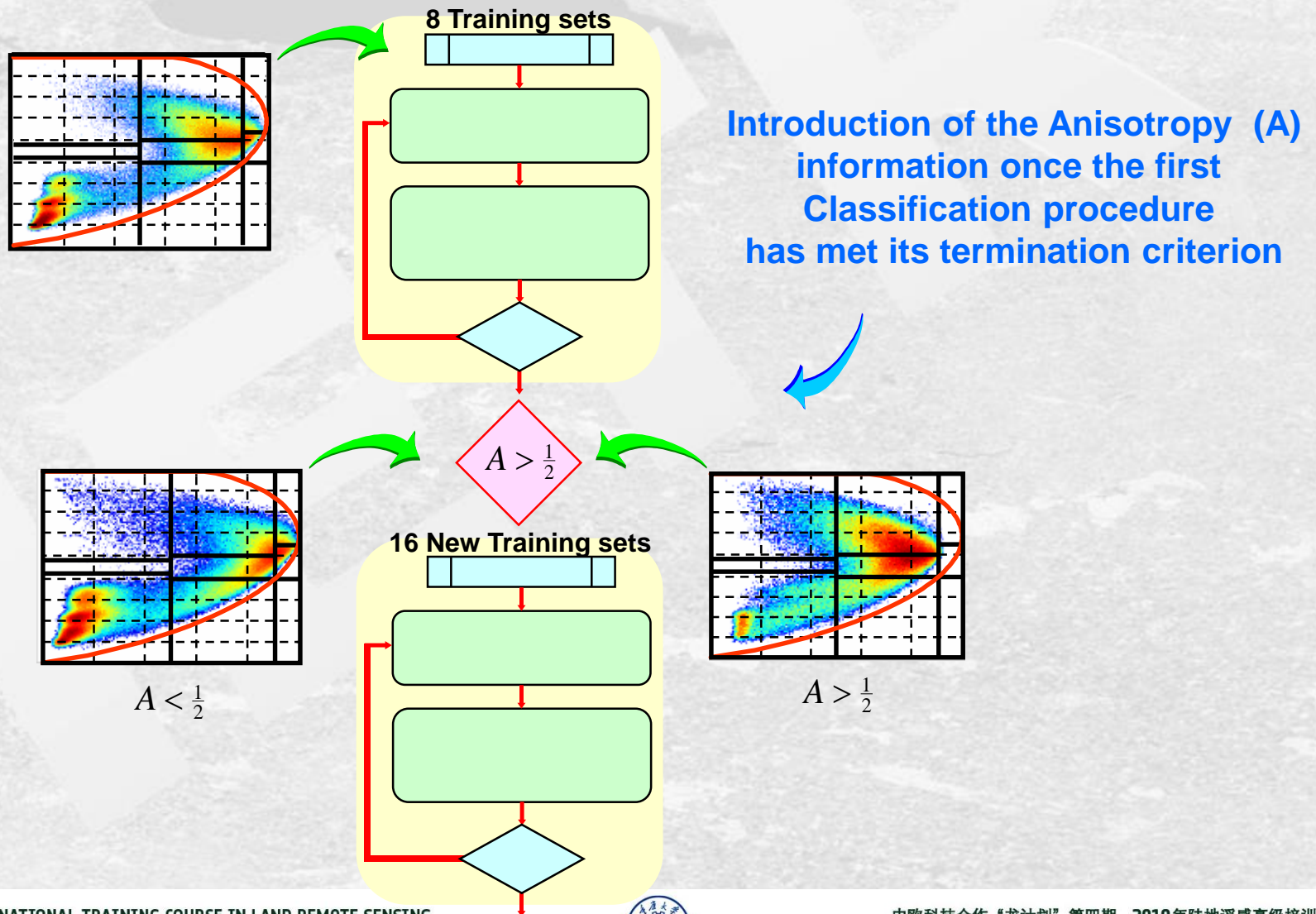


## POLSAR DATA DISTRIBUTION IN THE H / A / $\alpha$ SPACE



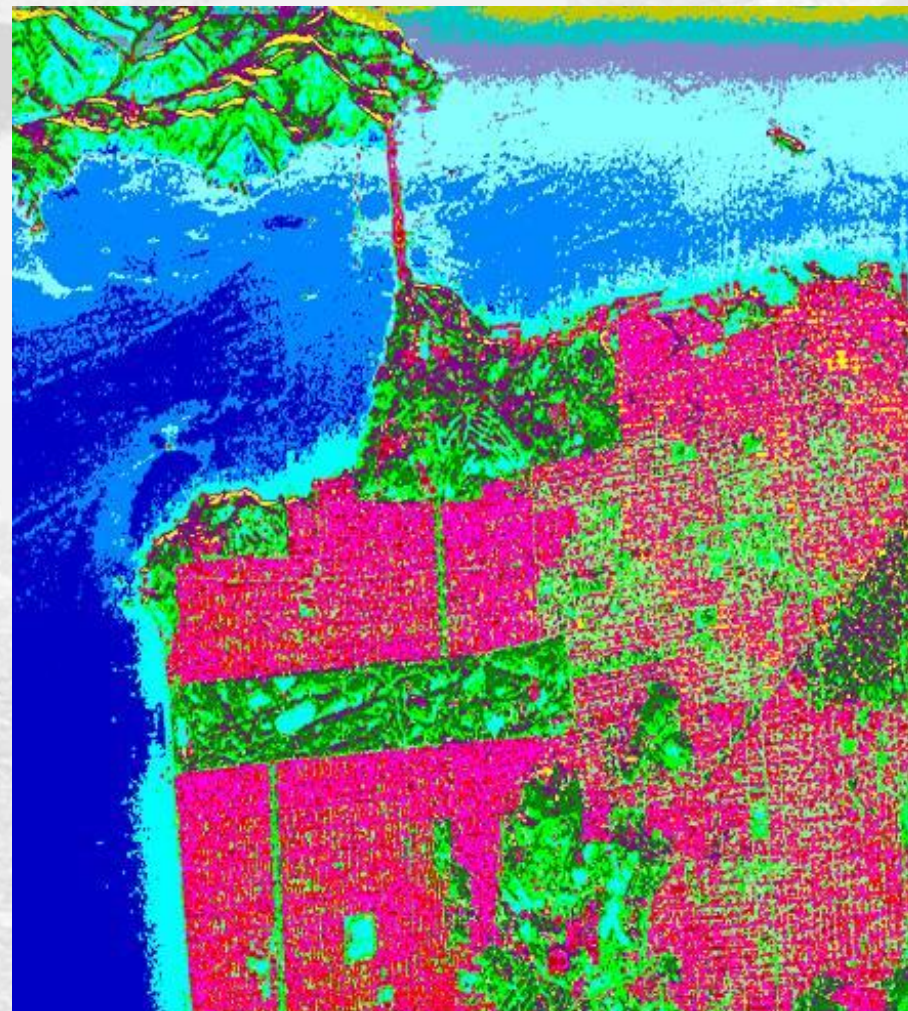


## 2 Successive k - mean Classification procedures



SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

4th ITERATION



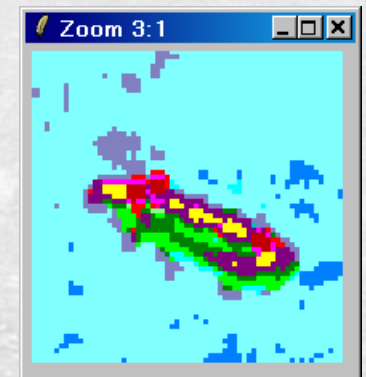
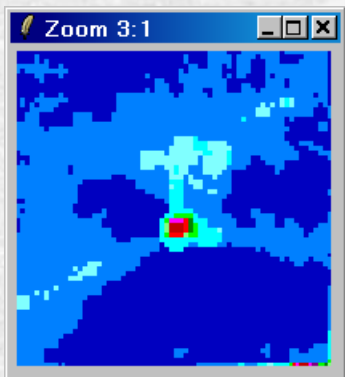
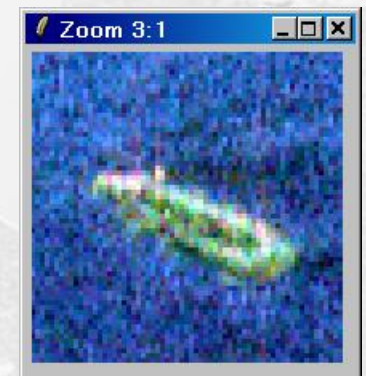
$2A_0$

$B_0 + B$

$B_0 - B$



## SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

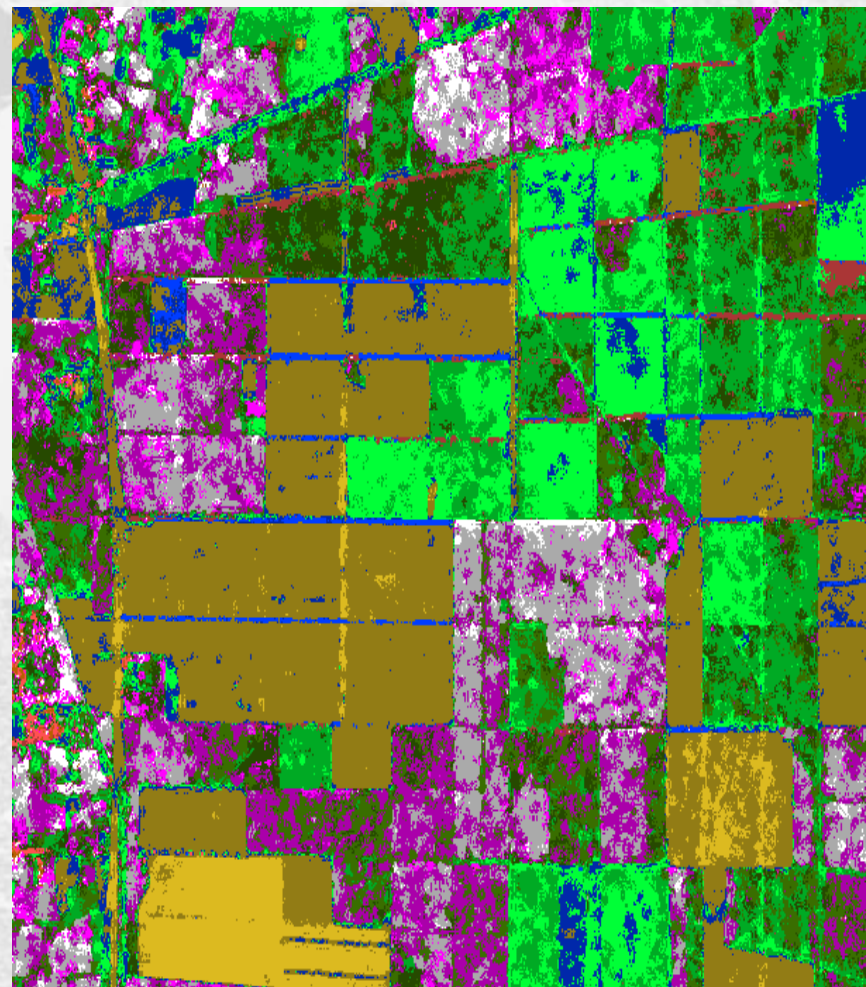


$$2A_0$$

$$B_0 + B$$

$$B_0 - B$$

## NEZER FOREST JPL - AIRSAR L-band



$2A_0$

$B_0 + B$

$B_0 - B$

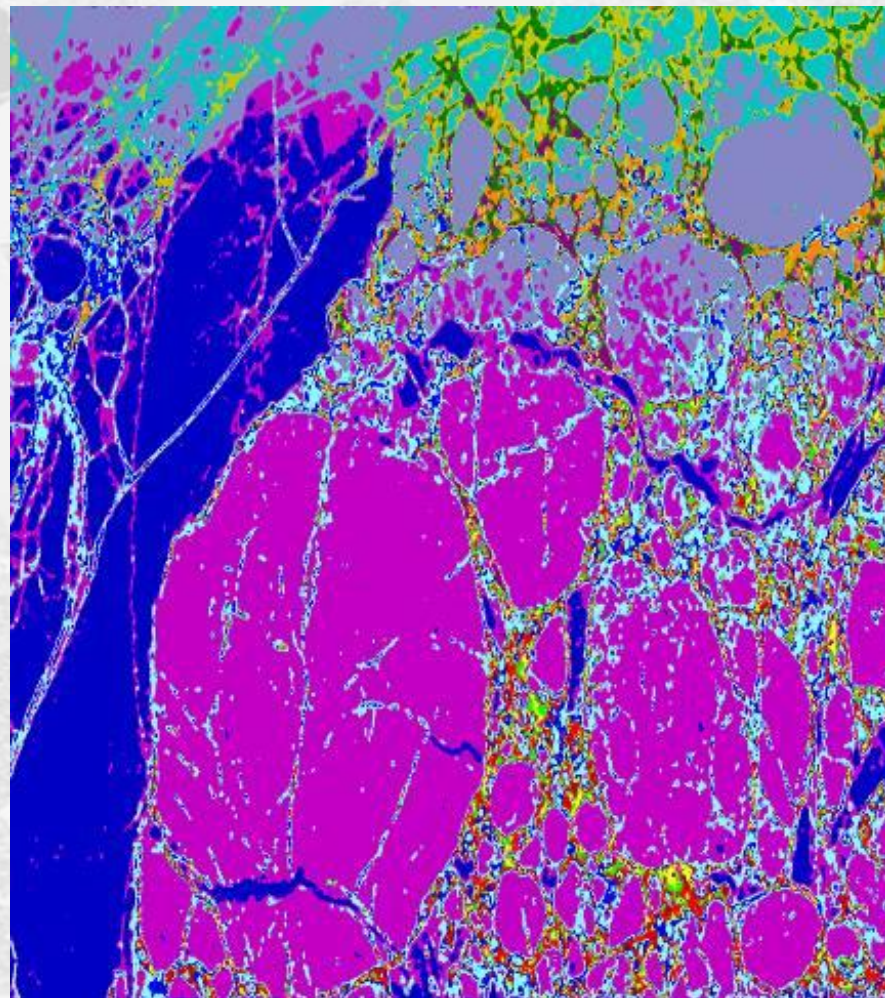
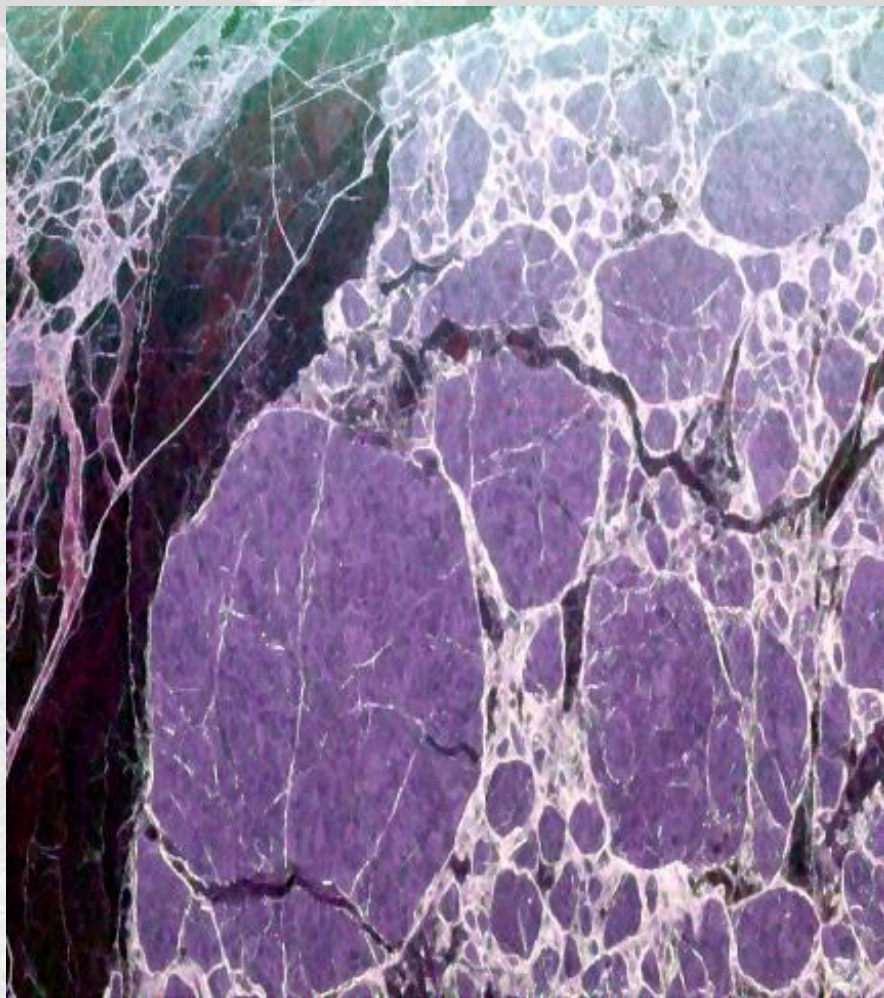
C1 C2 C3 C4 C5 C6 C7 C8



C9 C10 C11 C12 C13 C14 C15 C16



## ICE AREA JPL - AIRSAR L-band



$2A_0$

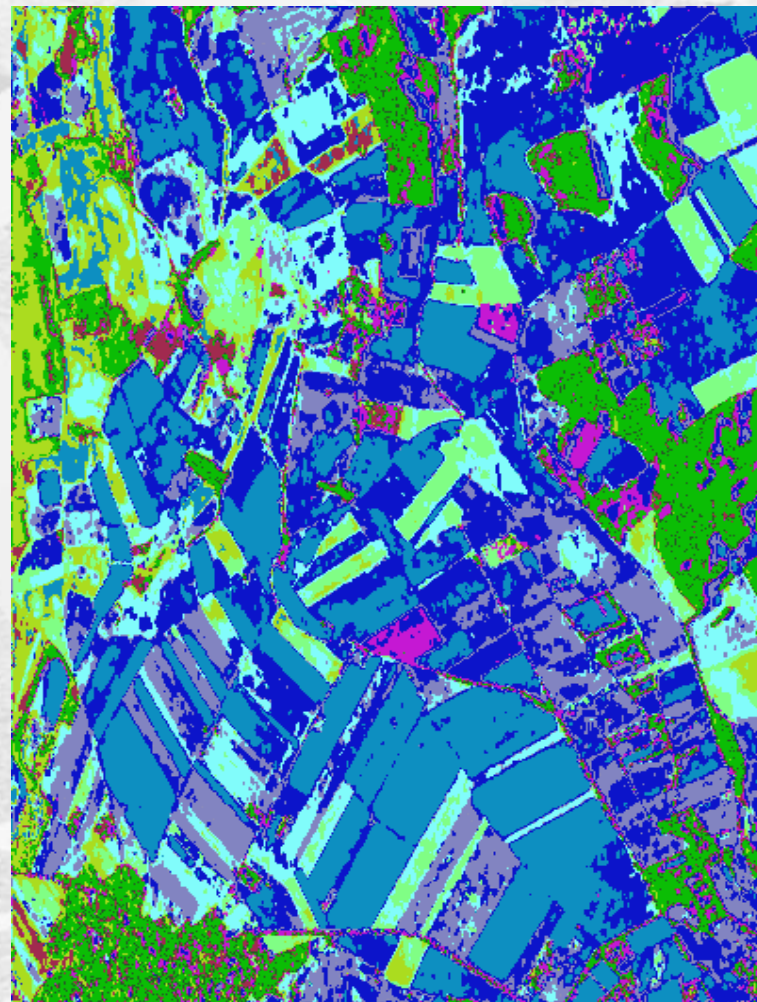
$B_0 + B$

$B_0 - B$



ALLING - ESAR L-band

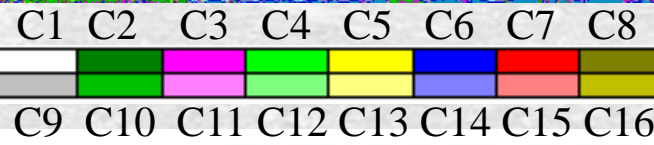
H / A /  $\alpha$  and WISHART CLASSIFIER



$2A_0$

$B_0 + B$

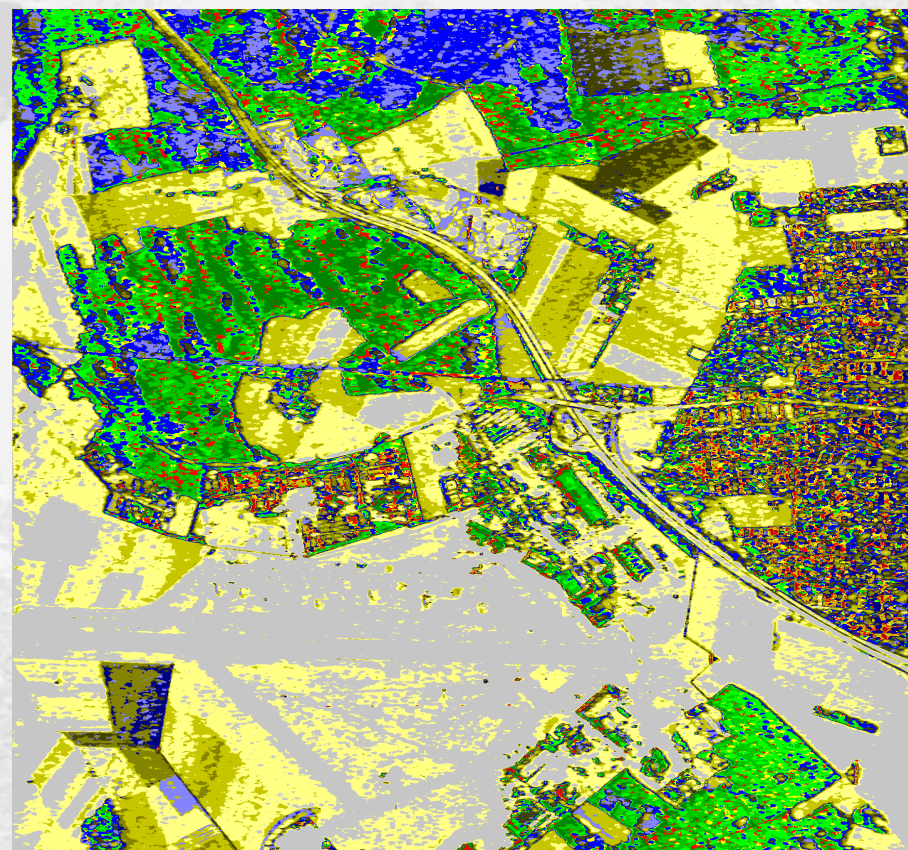
$B_0 - B$



## OBERPFAFFENHOFEN - ESAR L-band



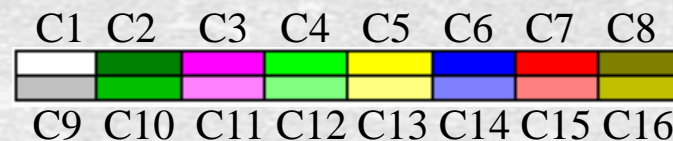
## H / A / $\alpha$ and WISHART CLASSIFIER



$2A_0$

$B_0 + B$

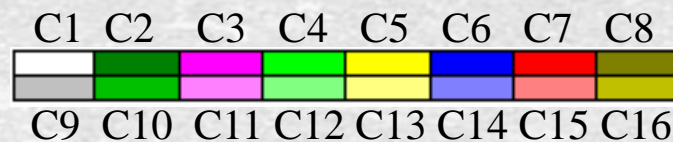
$B_0 - B$



OBERPFAFFENHOFEN - ESAR L-band



H / A /  $\alpha$  and WISHART CLASSIFIER



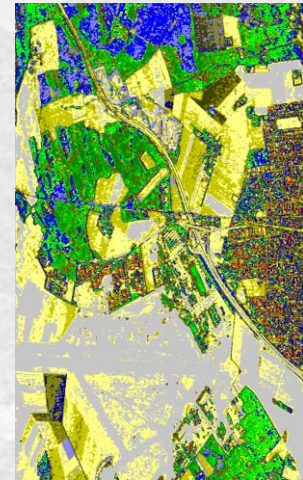


**WISHART PDF**  $P(\langle [T] \rangle / [T_m]) = \frac{L^p \langle [T] \rangle^{L-p} e^{-LTr([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$



## UNSUPERVISED POL SAR CLASSIFICATION

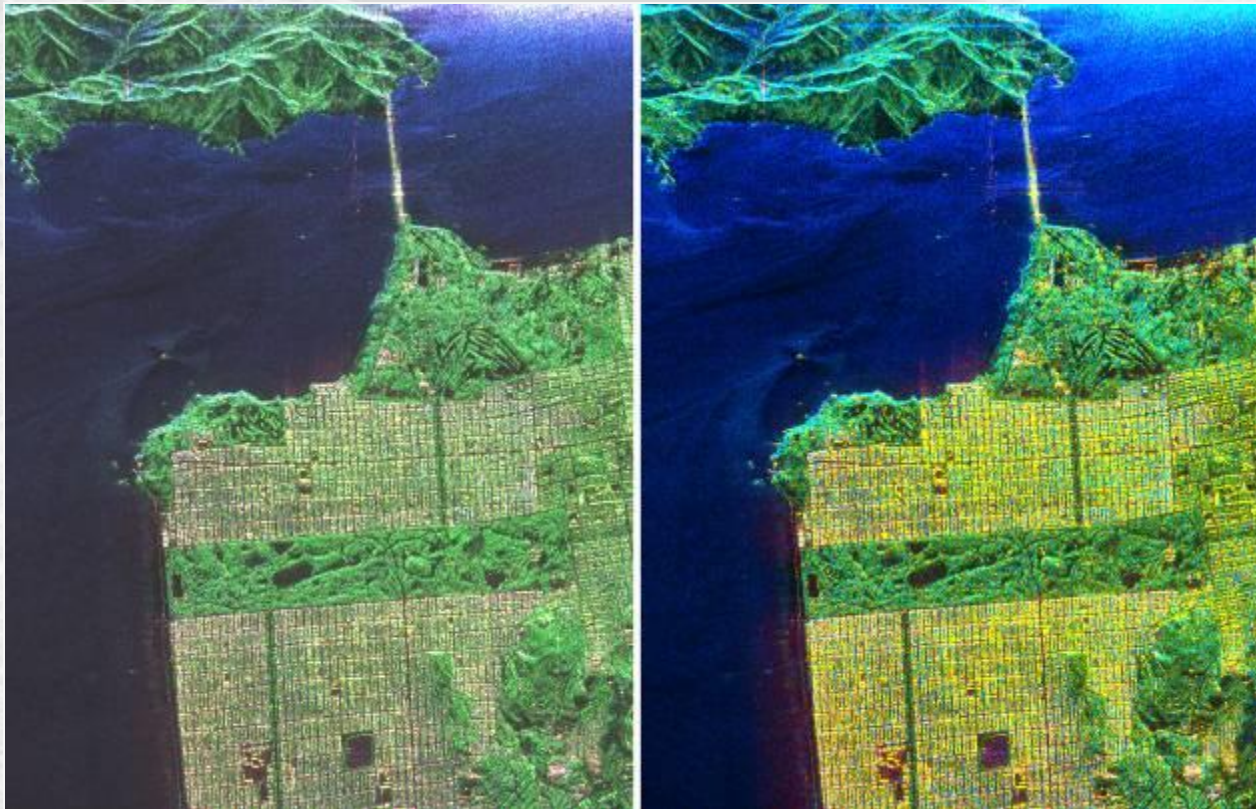
J.S LEE et al. (2002)



## Unsupervised Classification Preserving Scattering Mechanisms

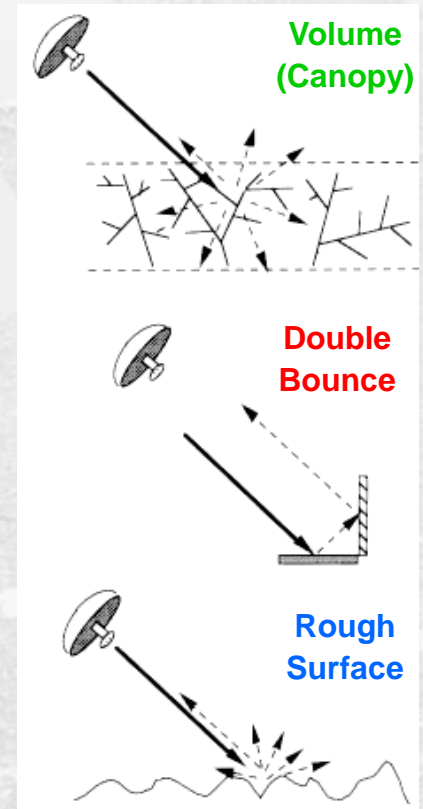
*J.S. Lee, M.R. Grunes, E. Pottier and L. Ferro-Famil, "Segmentation of polarimetric SAR images that preserves scattering mechanisms" Proceedings of EUSAR2002*

Courtesy of Dr J.S Lee

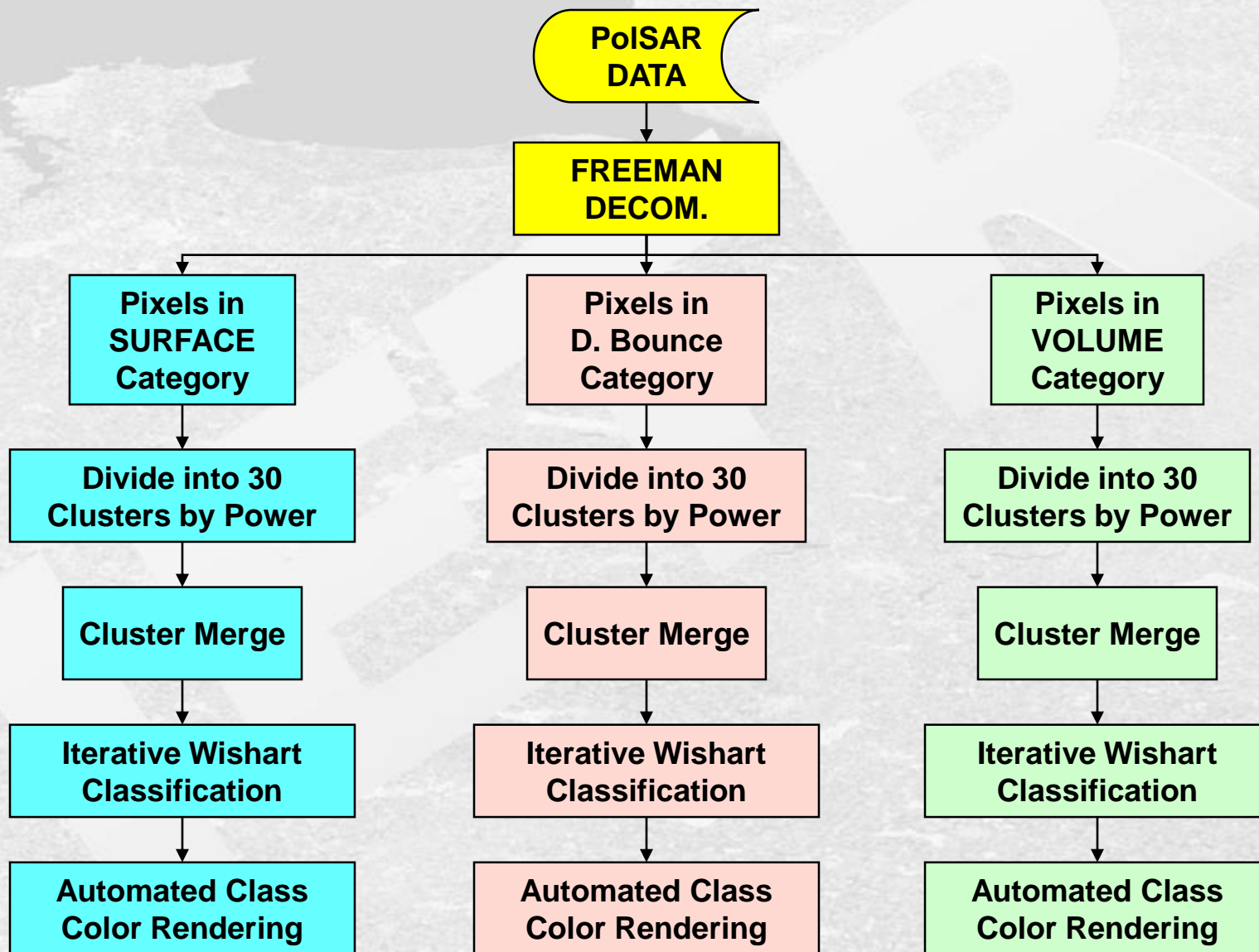


$|HH-VV|$ ,  $|HV|$ ,  $|HH+VV|$

Freeman and Durden



A. Freeman and S.L. Durden, "A Three-Component Scattering Model for Polarimetric SAR Data" IEEE TGRS, vol. 36, no. 3, May 1998



Cluster Merging  $D_{ij} = \frac{1}{2} \{ \ln(|V_i|) + \ln(|V_j|) + \text{Tr}(V_i^{-1}V_j + V_j^{-1}V_i) \}$

## Wishart Iteration – After Class Merge

### Classification Maps



First Iteration



Second Iteration



Third Iteration

**Note: Stability insures good convergence**

Courtesy of Dr J.S Lee



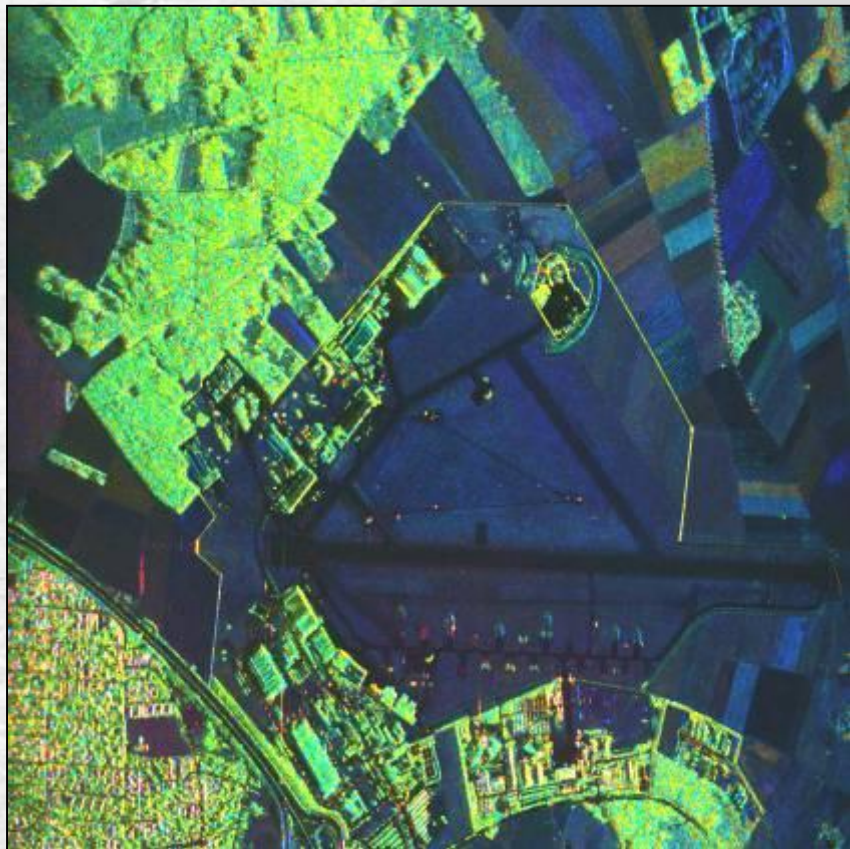
$|HH-VV|$ ,  $|HV|$ ,  $|HH+VV|$



4<sup>th</sup> Iteration (15 classes)



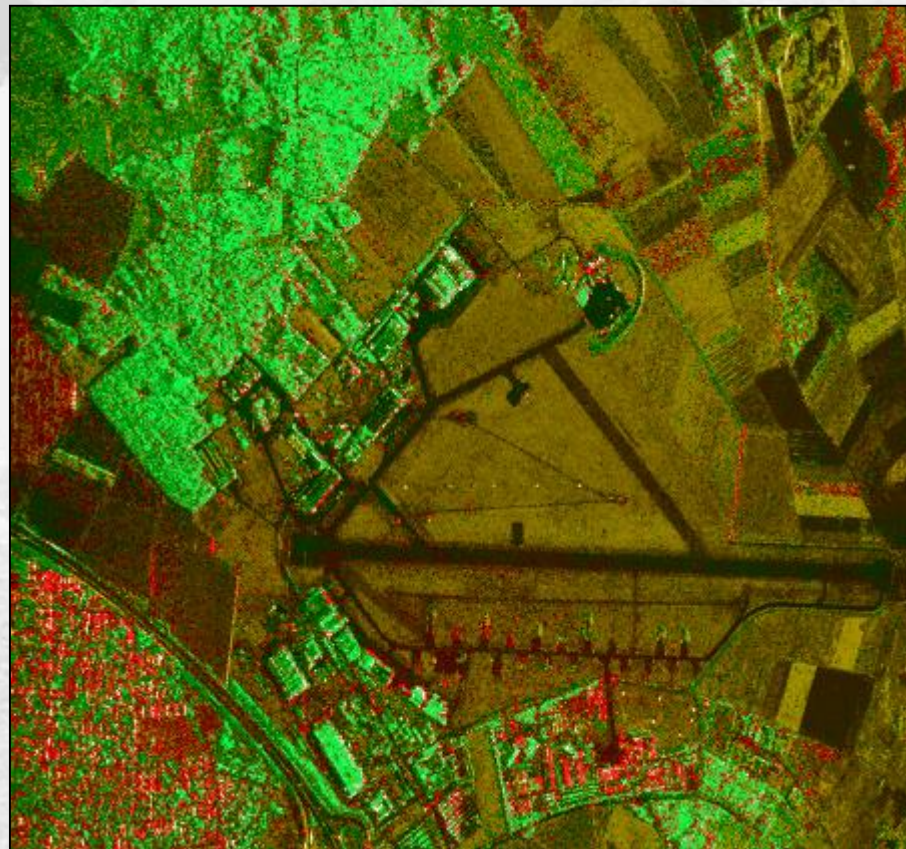
Courtesy of Dr J.S Lee



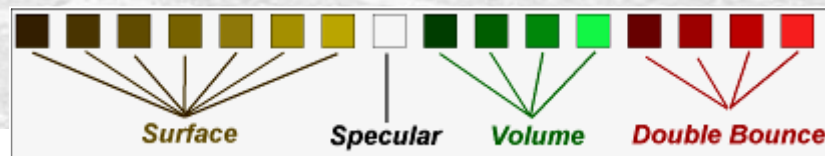
$2A_0$

$B_0 + B$

$B_0 - B$



4<sup>th</sup> Iteration (15 classes)



Courtesy of Dr J.S Lee

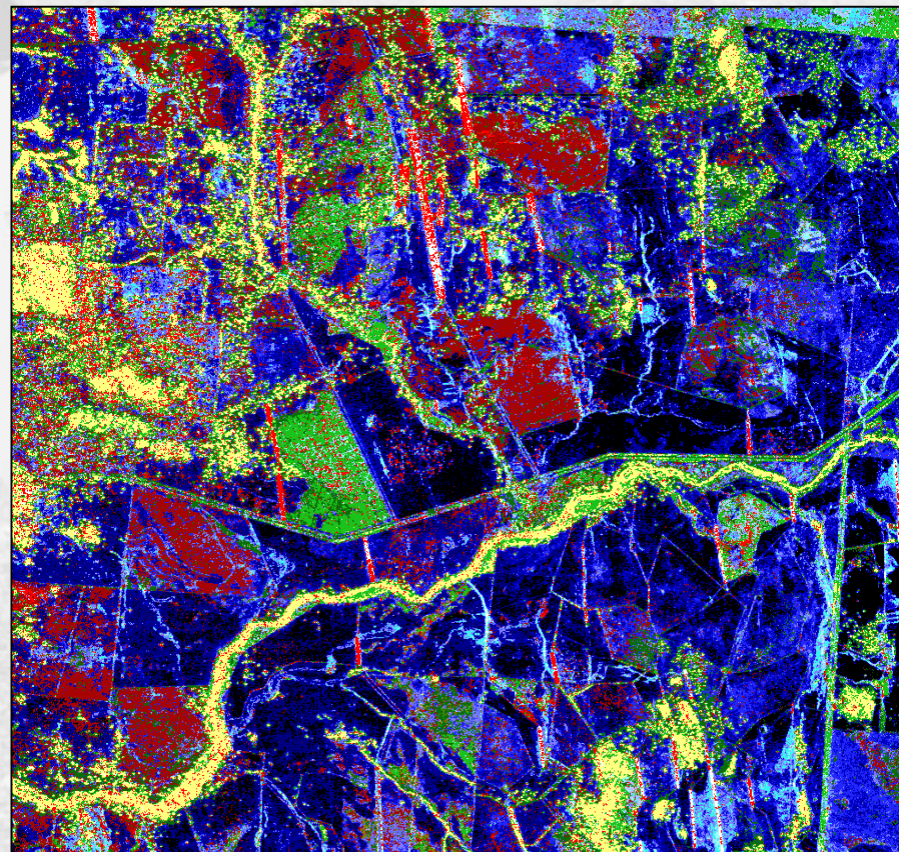


$2A_0$

$B_0 + B$

$B_0 - B$

**Australian Pasture**



4<sup>th</sup> Iteration (15 classes)



**L-Band Volume Dominated**

# Questions ?





# Books On Polarimetric Radar SAR, Polarimetric Interferometry

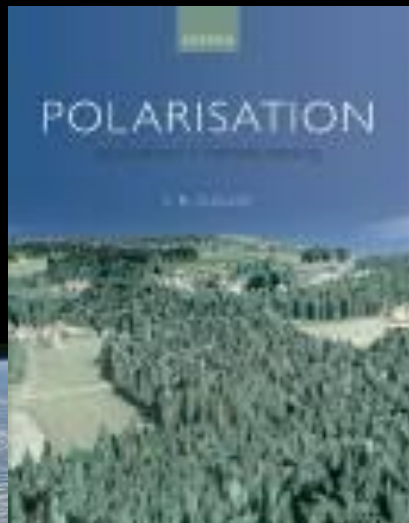


## **Polarimetric Radar Imaging: From basics to applications**

**Jong-Sen LEE – Eric POTTIER**

CRC Press; 1st ed., February 2009, pp 422

ISBN: 978-1420054972



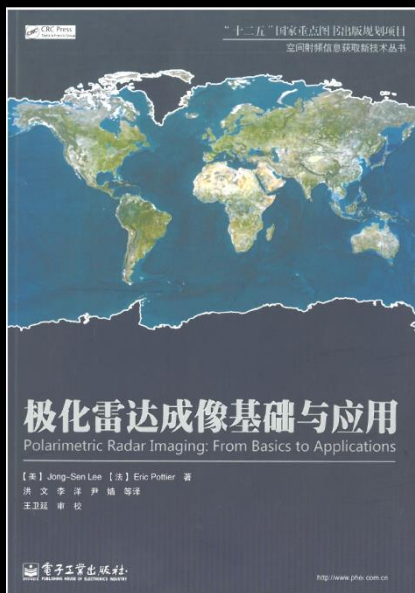
## **Polarisation: Applications in Remote Sensing**

**Shane R. CLOUDE**

Oxford University Press, October 2009, pp 352

ISBN: 978-0199569731

# Books On Polarimetric Radar SAR, Polarimetric Interferometry



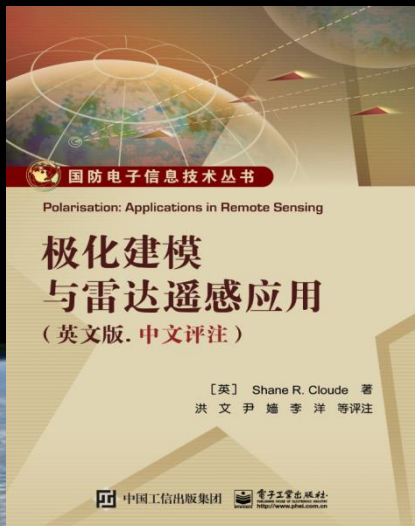
## Polarimetric Radar Imaging: From basics to applications

*Jong-Sen LEE – Eric POTTIER*

CRC Press; 1st ed., February 2009, pp 422

ISBN: 978-1420054972

*Prof. Wen HONG, Dr. Qiang YIN et al.*



## Polarisation: Applications in Remote Sensing *Shane R. CLOUDE*

Oxford University Press, October 2009, pp 352

ISBN: 978-0199569731